ENERGY MEASUREMENT

Energy can be defined as the capacity to do work, while power can be defined as the rate of doing work. There are different types of energy, including electrical energy, heat energy, nuclear energy, and solar energy. Energy may be converted from one form to another; for instance, electricity is often generated in power plants by converting hydraulic or fuel energy into electrical energy. Most vehicles are driven using energy derived from hydrocarbon fuels, and cooking is often done using electrical energy. Figure 1 shows the rapid increase of energy consumption in recent decades which helps us to get an idea of our ever increasing dependence on energy. Therefore, energy measurement becomes an extremely important topic for scientists and engineers. In this article, we will deal with different aspects of electrical energy measurement. Generally speaking, the measurement of energy is essentially the same as the measurement of power, except that the instrument must not merely indicate the power, but must take into account the length of time for which this power supply is maintained (1). Energy meters can be broadly classified into (1) electrolytic meters, (2) clock meters, (3) motor meters, and (4) electronic or microprocessor-based meters.

as the product of voltage and current, that is,

$$
P = VI \tag{1}
$$

where *V* is the dc voltage in volts and *I* is the dc current in power is expressed in vars (volt-amperes reactive).
supports The direction of positive current flow is defined to Energy is defined as the total work done flows from a point of higher voltage or potential to a point of use and larger units such as kilowatt-hour lower voltage. Since V or I may be either positive or negative $Eq. (2)$, the dc energy can be expressed as lower voltage. Since V or I may be either positive or negative, power may itself be positive or negative. Positive power implies power delivered to a device or load, while negative power E_d implies that power has been generated, that is, converted from some other form to electrical. Electrical power is typi- Using Eq. (5), the total energy delivered during time interval cally expressed in watts. *T* can be expressed as

In many systems the voltage and current are proportional, and are related by Ohm's law, $V = IR$, where *R* is the load

resistance in ohms. Using Ohm's law, Eq. (1) may be rewritten as

$$
P = I^2 R \tag{2}
$$

If the voltage and current vary with time, the instantaneous power (*p*) is defined as

$$
p = vi \tag{3}
$$

where *v* is the instantaneous voltage and *i* is the instantaneous current. Typically power is distributed to consumers in sinusoidal form, so that both the voltage and current are assumed to be sinusoidal and have the same frequency. An important measure of power, especially for periodic voltages and currents, is called average power. The average power is equal to the average rate at which energy is absorbed by an element, and it is independent of time (2). This is the power monitored by the electric utility company in determining monthly electricity bills. The average power (P_a) associated with a periodic instantaneous power signal is given by

$$
P_{\rm a} = \frac{1}{T_{\rm p}} \int_{t_0}^{t_0 + T_{\rm p}} p \, dt = \frac{1}{T_{\rm p}} \int_{t_0}^{t_0 + T_{\rm p}} vi \, dt \tag{4}
$$

where T_p is the period of both *v* and *i*, and t_0 is arbitrary. If the effective or root mean square (rms) values of the instantaneous voltage *v* and instantaneous current *i* are denoted by *V* and *I*, and the phase angles of the voltage and current are θ_{ν} and θ_{i} , then the average power delivered to the load is

$$
P_{\rm a} = |V| |I| \cos \theta \tag{5}
$$

where $\theta = \theta_v - \theta_i$ is the phase difference between v and i . The **Figure 1.** Graph depicting our increasing dependence on energy. factor $\cos\theta$ is called the power factor, and θ is the power factor angle. P_a is called real power, which implies that the power **HEORY** has transformed from electrical to nonelectrical form such as radiant, chemical, or mechanical. If the load is purely re-
Referentively property measurement itself let us mathe-
sistive, the voltage and current sig Before discussing energy measurement itself, let us mathe-
matically define electrical energy with respect to power. This
matically define electrical energy with respect to power. This
will help us to understand energy me

$$
Q = |V| |I| \sin \theta \tag{6}
$$

where the factor $\sin \theta$ is called the reactive factor. Reactive

amperes. The direction of positive current flow is defined to Energy is defined as the total work done over an interval
be the direction a positive charge flows (or would flow if possi- of time (T) , and the basic unit of be the direction a positive charge flows (or would flow if possi- of time (T) , and the basic unit of energy is called the joule or ble), and positive power is delivered when positive current watt-second. In many instance ble), and positive power is delivered when positive current watt-second. In many instances, this unit is inconvenient to flows from a point of higher voltage or potential to a point of use and larger units such as kilowatt

$$
E_{\rm d} = I^2 R T \tag{7}
$$

$$
E_{\rm a} = |V| |I| T \cos \theta \tag{8}
$$

Similarly, using Eq. (6), the reactive energy can be expressed as **Electrolytic Watt–Hour Meters**

$$
E_r = |V| |I| T \sin \theta \tag{9}
$$

of large amount of electric energy are accomplished by means of three-phase circuits. A comprehensive analysis of threephase circuits is beyond the scope of this article; a general understanding of balanced three-phase circuits is sufficient for our purpose. The basic structure of a three-phase system consists of voltage sources connected to the loads by means of transformers and transmission lines. Figure 2 shows the simplified block diagram of a basic three-phase circuit. A set of balanced three-phase voltages consists of three sinusoidal voltages that have identical amplitudes and frequency but are out of phase with each other by exactly 120°. In three-phase circuits the standard practice is to refer to the three phases as A, B, and C. Furthermore, phase A is almost always used as the reference phase. Because the phase voltages are out of phase by 120° the following two possible relationships can exist between the voltages:

First Possibility.
$$
V_A = V_m \angle 0^\circ
$$
, $V_B = V_m \angle -120^\circ$, $V_C = V_m \angle +120^\circ$
\nSecond Possibility. $V_A = V_m \angle 0^\circ$, $V_B = V_m \angle +120^\circ$, $V_C = V_m \angle -120^\circ$

Here V_m represents the peak amplitude of the sinusoidal voltage. The energy delivered by a three-phase source and consumed by a three-phase load is found simply by adding the energies in the three phases. In a balanced three-phase circuit, however, this is the same as multiplying the average energy in any one phase by 3, since the average energy is same in all phases. Thus for a balanced three-phase circuit the active energy or energy may be expressed as

$$
E_{\rm a} = 3V_{\rm p}I_{\rm p}T\cos\theta_{\rm p} \tag{10}
$$

where V_p represents the magnitude of the phase voltage, I_p represents the magnitude of the phase current, and θ_{p} represents the phase difference between V_p and I_p . Similarly, the total reactive energy can be expressed as

$$
E_r = 3V_p I_p T \sin \theta_p \tag{11}
$$

In the case of energy the measuring instrument is called a watt–hour meter, while in the case of reactive energy the **Figure 3.** Electrolytic watt–hour meter. A, anode mercury; B, glass measuring instrument is called a reactive volt-ampere-hour fence; C, cathode; D, negative terminal; E, positive terminal; K, meter. shunt; H, compensating resistance in series with tube.

WATT–HOUR METERS

A meter that records energy in watt-hours or kilowatt-hours is called a watt–hour meter. An important requirement of an energy meter is that it should indicate a given amount of energy proportional to power and time. For example, it should record 1 kW \cdot h, whether this consists of 1 W flowing for 1000 h or 1000 W flowing for 1 h. Different types of watt–hour Figure 2. A basic three-phase circuit. meters have been developed in the last few decades for the measurement of energy. We shall briefly discuss only those that are relevant today.

Figure 3 shows an electrolytic watt–hour meter. This type of meter is mainly used for dc energy measurement, although it can be adapted, by using a metal rectifier circuit and a cur- The generation, transmission, distribution, and utilization

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rent transformer, to function as an ac circuit for measuring kilovolt-ampere-hours. The operating current is passed through a solution, causing electrolytic action. Depending on the meter type, this gives a deposit of mercury or liberates gas proportional to the number of coulombs or ampere-hours passed through the meter. Assuming the voltage supply to the meter remains constant, the meter can be calibrated in kilowatt-hours; otherwise it is calibrated in ampere-hours. These meters are inexpensive to manufacture, but tend to require fairly frequent inspection, as they include a large amount of glass in their construction.

Clock Watt–Hour Meters

Figure 4 shows a clock watt–hour meter. There are two identical circular coils (C1 and C2), placed at the bottom ends of **Figure 5.** Motor watt–hour meter for dc energy measurement. two pendulums, which are continuously driven by clockwork. These coils are connected in series with one another and with

a high resistance, and they carry a current proportional to

a high resistance, and they carry a current proportional to

the line woldge. There are two curre tional to the energy passing through the meter. This meter is **Single-Phase Induction Watt–Hour Meter.** Induction meters

comparatively free from temperature errors and stray fields are almost universally used for ac energy measurement, since
and is suitable for both ac and dc energy measurements. they are simple in construction, provide high ratio, and are relatively inexpensive. An induction watt–hour **Motor Watt–Hour Meters** meter consists of an induction motor whose output is largely absorbed by the braking disk and dissipated as heat as shown Motor watt–hour meters can be broadly divided into two cate- in Fig. 6. In this watt–hour meter there are two current poles gories: those for dc and for ac energy measurement. The lat- (2 and 4), which are displaced from the voltage pole (3) as ter—also called induction watthour meters—can be further shown in Fig. 6(a). At unity power factor, the flux ϕ_i from the classified into single-phase and polyphase watt-hour meters. current coils is in phase both with current coils is in phase both with the voltage v and current *i*. The flux from the voltage coil, ϕ_v , is in quadrature (90^o) **Motor Watt-Hour Meter for dc Energy Measurement.** A motor
meter for dc energy measurement essentially consists of a
small motor that is provided with a magnetic braking mecha-
 ϕ_i is minimum. The flux paths through the 1, from 2 to 3, from 3 to 4, and from 5 to 4. At time instant *b*, both the current *i* and current flux ϕ_i are minimum, but the voltage v is minimum and the voltage flux ϕ_v is maximum. At time instant *c*, both the current *i* and current flux ϕ_i are maximum, but the voltage v is maximum and the voltage flux ϕ_n is minimum. The flux paths through the disk are from 1 to 2, from 3 to 2, from 4 to 3, and from 4 to 5. Thus the flux has effectively moved across the disk from left to right. This change causes eddy currents to be set up in the disk. The reaction between the eddy currents and the field tends to move the disk in the direction of the field.

> Since the disk revolves continuously when on load, electromagnetic forces (emfs) will be induced in it dynamically, as it cuts through the flux between the poles, in addition to the statically induced emfs due to the alternating flux in these poles. The torque due to the dynamically induced eddy cur-**Figure 4.** Clock watt–hour meter. rents in the disk will be negligible compared to the operating

Figure 6. Induction watt–hour meter for ac energy measurement.

$$
T_{\rm d} \propto |V| |I| \cos \theta \tag{12}
$$

$$
N \propto |V| |I| \cos \theta \tag{13}
$$

i.e., the speed of revolution of the disk is proportional to the power. The total number of revolutions, N_T , over a time inter-
val T may be expressed as
proposed as
f a

$$
N_{\rm T} = NT = |V| |I| T \cos \theta \tag{14}
$$

method of energy measurement. gram of a microprocessor-based energy measurement system

torque produced by the statically induced currents. Neglect- instruments, however, utilize two or more single-phase eleing the effect of friction in the meter, and assuming that the ments mounted in a single shaft, which drives the dial. These active flux from the voltage pole lags 90° behind the impres- elements must be shielded from each other to avoid interacsed voltage, the operating or driving torque *T*^d becomes pro- tion between the fluxes produced by individual elements. For portional to the power in the circuit, i.e., instance, three-phase energy can be measured by having three watt–hour meters with current coils in each line and potential coils connected across the given line and any com-Now the retarding torque T_r due to eddy currents is propor-
tional to the speed of revolution, N, of the disk, i.e., $T_r \propto N$.
Since the common junction is completely arbitrary, it may be placed in any of the three line Since for a steady speed of the disk, T_d must be equal to T_r , done, the wall-nour meter connected in that line will indicate
we can write the disk, T_d must be equal to T_r , and the value of the step of the step of with, and the three-phase energy can be measured with only two watt–hour meters. In general, *m*-phase energy can be measured by $m - 1$ watthour meters.

sure appropriate connection of the various components of a polyphase watt–hour meter for registering accurate results. In a three-phase circuit, when the power factor is 1 corre-From Eq. (14), it is evident that the total number of revolu-
tions is proportional to the total energy supplied.
tion will be in the forward direction at the same speed. If the **Polyphase Induction Watt–Hour Meter.** Polyphase energy power factor is above 0.5, the disk rotation will always be can be measured by several single-phase instruments, since forward whenever the current or the potential coil of either of the total power or energy is the sum of the readings of all the two watt-hour meters is disconnected. On the other hand, instruments. The connections to the polyphase meters are the if the power factor is less than 0.5, the disk rotation of the same as those employed in the two wattmeter method of mea- two watt-hour meters will be in the opposite directions. It suring three-phase power, as shown in Fig. 7. Most polyphase should be mentioned that if the current coils of the two watt– hour meters of Fig. 7 are interchanged and the power factor is 0.5, the meter reading will be 100% wrong although it will run at normal speed.

> *Induction Watt–Hour Meter Adjustments.* All adjustments of induction watt–hour meter are usually made either at full load or at light load. To adjust the speed at full load, the drag magnet is usually shifted relative to the disk axis. Alternatively, speed adjustments can be made by using a movable soft iron bar for shunting the flux. To compensate for variations in ambient temperature, a small piece of temperaturesensitive iron–nickel alloy is generally used as a shunt in the air gap of the drag magnets.

MICROPROCESSOR-BASED ENERGY METERS

Microprocessor-based systems are increasingly being used in **Figure 7.** Connection diagram for polyphase watt-hour meter energy measurement. Figure 8 shows the simplified block dia-

Figure 8. Simplified block diagram of a microprocessor-based energy meter.

an analog unit and a digital unit. The input signals *v* and *i* shifting in sampling meters, and electronic integrators in are multiplied in an analog multiplier. An analog integrator, time-division multiplier meters are used (5). If the voltage such as a dual slope converter, performs integration on the across the single-phase circuit is given by multiplier output signal over a time interval T_i . The microprocessor sends a start pulse of suitable duration to activate the synchronization circuit. The synchronization circuit, after synchronization with the input signal *v*, generates a signal of then the voltage in quadrature is given by duration T_i , which controls the time counter gating logic. Notice that *T*_i is the period of integration for the multiplier output signal and is always equal to an integer multiple of the input signal period. Subsequently, the analog integrator inte- From the point of view of measuring system design, it is irrelgrates a reference signal over a period T_i , which is measured evant whether the phase shift is performed on the voltage or by the time counter. The microprocessor keeps track of the on the current signal. Only the phase displacement between entire duration (T) of measurement using an internal counter. the input signals is of importance. Figu entire duration (T) of measurement using an internal counter. the input signals is of importance. Figure 9 shows the simpli-
The outputs of the event and time counters are fed into the fied block diagram of a reactive po The outputs of the event and time counters are fed into the fied block diagram of a reactive power and energy measure-
microprocessor system, which internally calculates the total ment system. At first, the voltage signal microprocessor system, which internally calculates the total ment system. At first, the voltage signal is given a 90° phase
energy and outputs the calculated or measured energy on the shift in the phase shifter; it is then energy and outputs the calculated or measured energy on the shift in the phase shifter; it is then multiplied with the cur-
display. With microprocessor-based energy meters, an accu- rent signal in the analog multiplier. T display. With microprocessor-based energy meters, an accuracy of the order of 0.1% can be achieved. the multiplier unit, that is, the reactive power signal, is intro-

Reactive energy is defined as the quantity measured by a per-
fect watt-hour meter that carries the current of a single-
phase circuit and a voltage equal in magnitude to the voltage
across the single phase circuit but in ally more complex than active energy measurement because additional processing of input signals is necessary. The most **METER RATINGS** common reactive energy meters are watt–hour meters with the currents through the voltage coils displaced by 90. To The rise in temperature resulting from the losses in a meter

employing synchronous counting (3). The system consists of cross phasing, *RC* and *RLC* circuits, varformers, digital phase

$$
v = |V| \sin \theta_v \tag{15}
$$

$$
v = |V| \sin(\theta_v - 90^\circ) \tag{16}
$$

duced into an analog-to-digital converter (ADC). The integrat-**REACTIVE VOLT-AMPERE-HOUR METERS** ing unit inherent in any ADC provides the power integration step to generate the reactive energy, which after some inter-

provide this 90 phase shift various methods such as potential must be accounted for when rating a meter because meter

Figure 9. Simplified block diagram of an electronic reactive energy measurement system.

consequent deterioration of insulating materials surrounding tial service are three-wire, 240 V, and class 200 (6). These the current carrying conductors. In general, a general purpose meters are generally tested at two test load points: full meter should have a lower permissible temperature than a load (FL), which is defined as 30 A, and light load (LL), special purpose meter to accommodate a greater factor of which is defined as 3 A. In order to get an indication of safety. In the past, watt–hour meters were rated only at the how a meter performs over a load range of 0 to 200 A, the full load which is currently referred to as the test ampere test results at full load and light load are weighted to yield (TA) rating or test current rating. The TA rating is indicated an overall accuracy. The overall accuracy (OA) equation is on the nameplate by the manufacturer and is mainly used written as for test constant calculation as well as for determining and adjusting the percent registration of a meter at light and heavy loads. The percent registration of a watt–hour meter is defined as the ratio of the actual registration to the value of
the quantity measured during a given time interval. Cur-
rently watt-hour meters are rated into a number of classes
based on their maximum capacities. A class

RECENT TRENDS

is one of the latest electronic gadgets to help us with energy measurement. Until recently a meter could only be tested by **CALIBRATION** pulling it and taking it back to the shop. However, portable testers effectively alleviated that problem. They are especially Phantom loading of watt–hour meters is a common method

ENERGY MEASUREMENT 109

life span should not be unduly shortened by overheating and Single-phase watt–hour meters typically used in residen-

$$
OA = \frac{4 \times FL + LL}{5}
$$
 (17)

$$
OA = \frac{FL + LL}{2}
$$
 (18)

Power and energy measurement using electronic systems, michared is not in widespread use.

croprocessors, and digital techniques is becoming increasingly
 $\frac{1}{2}$ Energy meters are also classified as *precise*

propular

helpful when customers live in remote areas. for their calibration. This mainly consists in supplying sources of calibration voltage that are independent of each other at one point and are adjustable. This practice has sev-**ACCURACY** eral advantages over the use of resistive and reactive loads, such as (1) better adjustment of voltage, current, and power Electric utilities all over the world use single-phase watt– factor in the laboratory, (2) reduced need for large current hour meters to measure residential energy consumption. supplies, and (3) elimination of errors that might result from Since the watt–hour meter serves as the cash register for the failure to take into account losses or loading effects in the utility, both the utility and the regulatory body have a high test and reference instruments. Figure 10 shows two circuits interest in its accuracy. In order to ensure that the customers commonly used in the calibration of watt–hour meters. In are not charged for more energy than they consume and the Fig. $10(a)$, the current circuits are connected in series and utility collects the revenue to which it is entitled, watt–hour supplied with a stepdown transformer for the test and refermeters are sampled on an annual basis, ensuring accurate ence instruments. This isolates the current circuit from the registration of energy. Typically the sampled meters are sent voltage circuit. A smaller series adjusting resistor may also to a central testing facility and tests are performed to indicate be used for adjusting the load current. This method is used how accurately the meters are performing in service. The re- when it is desired to simulate a unity-power-factor load. The sults of these sampled tests are reported to the regulatory voltage of the current supply transformer must be high body to satisfy its rules and regulations. The utility also uses enough so that it swamps the reactance of the current circuits statistical tools for determining the performance of the me- of the meters. The circuit in Fig. 10(b) is used when lowter population. power-factor loads of the order of 50 are desired. By using a

PORTABLE METER READING AND STANDARDS

Presently utilities all over the world are debating whether to **CONCLUSION** incorporate *automated meter reading* (AMR) in their systems. AMR offers many other advantages than just remote meter In this article we started off by defining some basic terms cording to the communication media used, whether they are of different aspects of energy measurement.

one-way or two-way, whether they read meters at high or low speed, and whether they are fixed or mobile. Utilities have been slow to adopt automated meter reading systems because the investment is high and the payback is slow. Other reasons include reluctance to change, discomfort with new technology, and long-term satisfaction with walkaround readers. Furthermore, AMR system requires a coordinated, horizontal effort across the utility, involving metering, billing, customer service, and information systems.

The most widely used technique for watt–hour meter testing is called portable standard or rotating standard. Portable standards are transportable watt–hour meters with multiple current and voltage range and allows both whole and fractional reading. Initially, energy is measured by using the watt-hour under test. Then the portable standard meter is used to measure the same energy. The accuracy is determined by comparing the readings of the two meters.

REFERENCE STANDARDS

For ac watt–hour meter testing, a time reference standard such as a clock or a stop watch and a wattmeter may be used. Alternatively, a watt–hour meter is used as the reference standard which is started and stopped automatically by a signal (e.g., light) generated from the meter to be tested. For dc watt–hour meter testing, the reference standard may be ammeters and voltmeters or potentiometers.

Standards and technical practices are an essential tool in any field, and energy measurement is no exception. In the USA, approximately half of all standards are generated through a voluntary consensus process (8). Most engineering standards are developed by technical societies and trade associations. The private sector rather than the government generates the standards. The American National Standards Institute (ANSI) coordinates the voluntary development of **Figure 10.** (a) A basic calibration circuit for a watt-hour meter, and
(b) a more sophisticated version of the calibration circuit.
societies. It is self-designated in its role in standard coordination and does not develop any standards. ANSI reviews the documents produced by others and certifies them as American three-phase supply and taking the current supply from one
phase and the voltage supply from another, it is possible to
simulate low-power-factor loads if the phase angle is known.
The phase for the voltage supply can be s ation (NFPA).

reading. An AMR system can signal outages, perform remote that would allow us to understand different aspects of energy connect and disconnect, deter meter tempering, prevent lock- measurement. We then described different types of energyouts, and facilitate time-of-use metering. In addition, utilities measuring instruments in detail, and briefly discussed some can offer value-added services such as forced-entry alarms of the latest trends in energy measurement. All these topics and low- or high-temperature alerts. Any of these can gener- were chosen by keeping in mind the diverse readership of this ate revenue. Over 30 vendors are in the AMR market, offering encyclopedia. With our present dependence on energy it is systems of every size and kind (7). The systems vary ac- necessary that a wide section of the population become aware

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