Static electricity is one of the earliest phenomena to be observed in physics. It aroused curiosity to understand the origin of the generation and movement of electrostatic charges. Contact electrification, or *triboelectric charging,* was discovered as early as 600 B.C. The investigation of static charges is the origin of our study of electricity: William Gilbert in the sixteenth century coined the term "electrical" from the Greek word for amber because amber and other resinous material charge so easily. During the seventeenth and most of the eighteenth century, the understanding of static electricity was primarily qualitative. However, a fundamental advance in our understanding of atmospheric static electricity was made by Benjamin Franklin. In the nineteenth century the pioneer studies on static electricity by scientists like Coulomb, Faraday, Maxwell, and Gauss laid the foundation of electrostatics. In the twentieth century, *current,* or flowing electricity, became an indispensable part of our daily lives in residential and industrial applications, from household appliances to transportation, from consumer electronics to supercomputers. However, the application of static electricity was not fully realized until late in the twentieth century. By then industrial electrostatic precipitators were widely used for gas cleaning and the electrophotographic process in copy machines and laser printers, which has become a billion dollar industry worldwide. Other major uses of static electricity include ink-jet printing, powder paint coating, electrostatic separation of impurities from minerals, and biomedical and pharmaceutical applications.

Along with the phenomenal growth of the semiconductor industry came concerns about the abatement of electrostatic discharge (ESD) in the development of circuit chips. During the last 50 years, a major effort has been focused on eliminating electrostatic charges, which are often a nuisance and in many cases extremely hazardous. A static discharge in many products may trigger explosions involving particulate materials. Electrical discharges can damage electronic circuitry, cause unwanted exposure of photographic films, and cause explosions during transfer of materials. Safety techniques and equipment have been developed for neutralizing static charge and to minimize industrial hazards. Several organic and inorganic materials are used as antistatic agents in carpet coatings and clothes drying.

Electrostatic processes are distinguished from electromagnetic processes in that electrostatic charges are stored in different media and the movement of the charges is either a discontinuous or a slow process. The associated magnetic fields are often negligible and are not considered.

To understand the electrostatic process, the fundamental concepts are discussed first. These concepts are related to

electrostatic charge, the coulombic forces of attraction and repulsion, the role of the dielectric constant of the medium in which charges are placed, the electric field and its relationship to the electric potential, Gauss's law, and Poisson's and Laplace's equations. These concepts are reviewed briefly in the following section. Most electrostatic processes involve charging and discharging. In order to explain the application of electrostatic processes, these mechanisms are discussed in the next two sections to provide an overview of the following topics: (1) charging of materials, (2) electrostatic atomization, (3) transport of charged particles, (4) deposition of charged particles, (5) separation of charged particles, (6) charge decay, (7) adhesion of charged particles, (8) electrostatic charges and electrostatic hazards, and (9) electrostatic charge neutralization. Applications are discussed in the subsequent sections: electrostatic precipita- Equation (2) shows that the coulombic force obeys an inverse tors, ink-jet printing, powder coating, electrophotography square law similar to that of gravitational and magnetic (copying machines and laser printers), electrostatic separa- forces. The unit of permittivity is the farad per meter. tion, and electrostatic hazard control. Additional books that provide excellent descriptions of these and other electro- **Dielectric Constant and Permittivity**

# $F$  **Electronic Charge**

The electrostatic charge  $q_e$  of a single electron is

$$
q_e = -1.602 \times 10^{-19} \text{ C}
$$
 (1)

where C stands for the unit of charge named after Coulomb. The charge on the electron is the smallest fundamental charge in electrostatics.

Coulomb's law describes the quantitative relationship of the means the electrostatic force between the charges is reduced<br>electrostatic forces between charged bodies. The force be-<br>tween like charges is repulsive, and that

$$
F_{\rm C} = \frac{q_1 q_2}{4\pi\epsilon_0 r^2} \tag{2}
$$

$$
\epsilon_0 = 8.854 \times 10^{-12} \text{ F/m} \tag{3}
$$



charges  $q_1$  and  $q_2$ .

**Table 1. Dielectric Constants of Some Common Materials**

Medium	Dielectric Constant
Free space (vacuum)	1.0
Air, most gases	$\approx 1.0$
Insulating oil	2.2
Plastics (polystyrene, nylon, Plexiglas,	$2.1 \text{ to } 3.5$
Teflon, etc.)	
$\operatorname{Water}$	80
Aluminum oxide	8.80
Titanium dioxide (rutile)	173 (perpendicular)
	86 (parallel)
Barium titanate	1200

If two charges are embedded in a dielectric medium, the coulombic force acting between them is reduced by the dimen-**FUNDAMENTAL CONCEPTS OF ELECTROSTATIC PROCESSES** sionless dielectric constant of the medium,  $\epsilon$ .

$$
F = \frac{q_1 q_2}{4\pi\epsilon_0\epsilon_r r^2} \tag{4}
$$

There is a decrease in the coulombic force and the electric field between the two charges because  $\epsilon \geq 1$  for all materials:

$$
F_{\rm e}(\text{dielectric material}) = \frac{F_{\rm e}(\text{vacuum})}{\epsilon_{\rm r}}\tag{5}
$$

**Coulomb's Law** For example, pure water has a dielectric constant of 80; this means the electrostatic force between the charges is reduced

ductors, charges are free to move until the potential difference between two points in the medium becomes zero. In a perfect insulator there is no flow of charges. The electric field where  $F_c$  is the coulombic force in newtons (N),  $q_1$  and  $q_2$  are<br>two charges separated by a distance r, and  $\epsilon_0$  is the permittiv-<br>ity of free space, given by<br>ity of free space, given by<br>two charges separated by a polarizability as the charges are displaced by the electric field. There is an induced charge on the surface as shown in Fig. 2. This induced charge appears on the surface across the medium when the electric field is applied. The induced charge per unit area is called the *displacement D*. Both electric field *E* and displacement field *D* are vectors related by the permittivity of free space and the dielectric constant of the medium  $(\epsilon_0 \epsilon)$ :

$$
\boldsymbol{D} = \epsilon_0 \epsilon_r \boldsymbol{E} \tag{6}
$$

**Figure 1.** Coulombic forces of attraction and repulsion between two The unit of *D* is in coulombs per square meter, whereas the



**Figure 2.** A thin layer of induced surface charge forms when a dielectric medium, placed in an electric field, polarizes.

The coulombic force experienced by a charge  $q_1$  due to a sec-The relationship between the potential *V* and the electric can be written as  $\frac{d}{dx}$  and  $\frac{d}{dx}$  and  $\frac{d}{dx}$  can be illustrated in a parallel plate capacitor as

$$
F = q_1 E \tag{7}
$$

where  $E$  is the electric field due to the presence of charge  $q_2$ . Therefore, the electric field *E* at a distance *r* due to a charge  $V_{AB} = -\int_A^B$ 

$$
E = \frac{q_2}{4\pi\epsilon_0\epsilon_r r^2}
$$
 (8) where

Equation (7) can be expressed in the vector form

$$
\boldsymbol{F} = q\boldsymbol{E} \tag{9}
$$

When there are more than two charges involved, the force glecting the boundaries. and the field are expressed as vector sum of the contributions from all other charges: **Electric Field Lines and Equipotential Surfaces**

$$
\boldsymbol{F} = \boldsymbol{F}_{12} + \boldsymbol{F}_{13} + \boldsymbol{F}_{14} + \boldsymbol{F}_{ij} \tag{10}
$$

$$
\mathbf{E} = \mathbf{E}_{12} + \mathbf{E}_{13} + \mathbf{E}_{14} + \mathbf{E}_{ij} \tag{11}
$$

where  $\mathbf{F}_{ij}$  and  $\mathbf{E}_{ij}$  represent the force and field, respectively, surrounding an object and held at a known potential. In some between charges  $q_i$  and  $q_j$ .

# **Electric Potential or Voltage**

The *electric potential* at a point is defined as the work done in moving a unit charge from infinity (where the potential is zero) to the point in question. Since work is defined as force times distance, the potential *V* can be written as

$$
V = \int \boldsymbol{E} \cdot d\boldsymbol{r}
$$
  
=  $-\int q\boldsymbol{E} \cdot d\boldsymbol{r}$  (12)

## **ELECTROSTATIC PROCESSES 17**

The negative sign arises because work is done on the unit charge  $(q = 1)$  to move it against the field **E** to the point in question. If the point is designated as *A*, then

$$
V_A = -\int_{\infty}^{A} q\boldsymbol{E} \cdot d\boldsymbol{r}
$$
 (13)

The potential difference  $V_{AB}$  between two points  $A$  and  $B$  can be written as

$$
V_{AB} = -\int_{A}^{B} q\boldsymbol{E} \cdot d\boldsymbol{r}
$$
 (14)

The potential *V* is a scalar quantity and not a vector like *E* and *dr*. Clearly, the electric field *E* is obtained from the voltage gradient, given by

$$
\mathbf{E} = -\frac{dV}{dr} = -\text{grad}V\tag{15}
$$

Using del, we can write

$$
E = -\nabla V \tag{16}
$$

field  $E$  can be illustrated in a parallel plate capacitor as shown in Fig. 3. A capacitor is formed by two parallel conduct- $F$  ing plates,  $A$  and  $B$ , separated by a distance  $d$ . The potential across the plates is given by

$$
V_{AB} = -\int_A^B \bm{E} \cdot d\bm{r} = Ed
$$

$$
E = -\frac{V_{AB}}{d} \tag{17}
$$

Figure 3 shows that the potential is constant everywhere on where  $\vec{F}$  is the coulombic force and  $\vec{E}$  is the applied electric the surface of a conducting plate. The electric field is constant the homogenous medium between the plates nethroughout the homogenous medium between the plates, ne-

*A* conducting electrode is an equipotential surface in space. The conducting surface has a large number of charges free to  $rearrange themselves so as to maintain a constant potential$ across the surface. A *Faraday cage* is a conductive surface



**Figure 3.** The potential difference and electric field across a parallel plate capacitor.



lines, and the broken curves represent equipotential surfaces. Since  $q$  is positive, the field lines are directed radially outward.

applications, the cage is a grounded screen (potential zero) and surrounds sensitive electronic equipment to protect it from being damaged by external electrostatic fields. A Fara-<br>day cage is often used for shielding electrostatic measure-<br>shape that encloses one or more charges. This is *Gauss's Law* day cage is often used for shielding electrostatic measure- shape that encloses one or more charges. This is *Gauss's Law,*

Electric field lines and equipotential surfaces can aid our visualization of electrostatic forces and movement of charged particles. Depending upon the geometry and location of elec trodes, the field lines and equipotential surfaces can be mapped according to the following criteria: From Eq. (6),  $\epsilon_0 \epsilon_i \mathbf{E} = \mathbf{D}$ ; therefore

- 1.  $E = -\text{grad } V = -\nabla V$ .
- 2. There can be no potential difference along a surface of
- 
- 
- 

The imaginary field lines and equipotential surfaces related charge from the measured electric field. to an isolated conducting sphere having a charge *q* are shown For example, if the charges are distributed uniformly, then in Fig. 4. Since all the points on the surface of the conducting within a volume *V* enclosed by a surface *S*, sphere are at the same potential, an equipotential surface close to the conducting surface must be parallel to it. The equipotential surfaces are shown as broken curves. The field lines (shown as solid lines) are perpendicular to the equipotential surfaces, and so are directed radially outward from the where  $q<sub>y</sub>$  is the total net charge per unit volume enclosed by positive conducting sphere. These lines represent the direction of the electric field.  $\qquad \qquad$  or the divergence, the divergence form of the above equation

Field lines always originate on charges and end on oppo- can be written as site charges. The density of the field lines represents the mag nitude of the electric field  $(E)$  caused by the charge.

# **Gauss's Law**

Let us consider the equipotential spherical surface of radius *r* as shown in Fig. 4. The field *E* at any point on the surface is given by Coulomb's law [Eq. (8)]:

$$
E = \frac{q}{4\pi\epsilon_0 r^2} \tag{18}
$$

The surface area *S* of the spherical shell of radius *r* is

$$
S = 4\pi r^2 \tag{19}
$$

The product of these two quantities is

$$
ES = \frac{q}{\epsilon_0} \tag{20}
$$

**Figure 4.** Field lines and equipotential surfaces related to an iso-<br>lated conducting sphere of radius  $r_0$ . The solid lines represent field written in the form

$$
ES = \frac{q}{\epsilon_0 \epsilon_r} \tag{21}
$$

or

$$
\epsilon_0 \epsilon_r = ES = q \tag{22}
$$

which can be written in the form

$$
\int_{S} (\epsilon_0 \epsilon_r \boldsymbol{E}) \cdot d\mathbf{S} = \sum q \tag{23a}
$$

$$
\int_{S} \mathbf{D} \cdot d\mathbf{S} = \sum q \tag{23b}
$$

a conductor.<br>Any point in grass can have only an<br>extential at ony surface of area *S*. Since *D* represents induced charge per unit 3. Any point in space can have only one potential at any<br>given instant of time.<br>4. Equipotential surfaces cannot intersect.<br>4. Equipotential surfaces cannot intersect.<br>4. Equipotential surfaces cannot intersect.<br>4. Equipo 5. Field lines are always perpendicular to equipotential electric field and the displacement can vary over the surface surfaces. **S**, but the integral of the product is the sum of all charges enclosed. Gauss's law can be used to calculate the field due to several charges distributed in space or to calculate the total

$$
\int_{S} \mathbf{D} \cdot d\mathbf{S} = \sum q = \int_{V} q_{v} dV \tag{24}
$$

the surface *S*. Since  $\int_{S} \mathbf{D} \cdot d\mathbf{S}/dV$  is the flux per unit volume,

$$
\nabla \cdot \mathbf{D} = q_{\rm v} \tag{25}
$$

$$
\nabla \cdot \boldsymbol{E} = q_{\rm v} \epsilon_0 \epsilon_{\rm r} \tag{26}
$$

## **Poisson's and Laplace's Equations**

Equation (16) showed the relationship between the electric potential *V* and the field *E*. In most cases, both *V* and *E* are functions of location  $(r)$ ; therefore, a general form of the same equation can be written as

$$
\boldsymbol{E}(\boldsymbol{r})=-\nabla V(\boldsymbol{r})
$$

We often need to estimate *V*(*r*) from the distribution of charge  $q_v$ . If we combine Gauss's law with the field–potential relationship, we can substitute Eq. (16) in Eq. (26):

$$
\nabla \cdot \mathbf{E} = q_{\rm v}/\epsilon_0 \epsilon_{\rm r}
$$

$$
\nabla \cdot (\nabla V) = -q_{\rm v}/\epsilon_0 \epsilon_{\rm r}
$$

$$
\nabla^2 V = -q_v/\epsilon_0 \epsilon_r \tag{27}
$$

Equation (27) is known as Poisson's equation. It can be used to calculate the potential distribution from the volume den-<br>Resistivity

In the regions where the net charge density is zero  $(q_v = 0)$  Poisson's equation becomes *Laplace's equation*:

$$
\nabla^2 V = 0 \tag{28}
$$

Most electrostatic processes can be analyzed using the re-<br>
rial, and  $R$  is the resistance in ohms.<br>
lationships above. Therefore, it is desirable to understand the There are two components of resistance lationships above. Therefore, it is desirable to understand the There are two components of resistivity: (1) volume resis-<br>physical concepts underlying Coulomb's law, Gauss's law, tivity a as defined above and (2) surface physical concepts underlying Coulomb's law, Gauss's law, tivity  $\rho<sub>v</sub>$  as defined above, and (2) surface resistivity  $\rho<sub>s</sub>$ . Both Poisson's equation, and Laplace's equation. To describe many are important since ch Poisson's equation, and Laplace's equation. To describe many are important, since charge can leak over the surface or electrostatic processes, the distribution of the electric field is through the material. The volume resi electrostatic processes, the distribution of the electric field is through the material. The volume resistivity is expressed in<br>often needed for a given electrode geometry. Once these ohm-meters The surface resistivity is boundary conditions and a knowledge of the volume charge square  $(\Omega/\square)$ .<br>distribution are specified, analytical and numerical tech-<br>many phe volume niques are available to solve Laplace's and Poisson's equa- als, as shown in Table 2. tions.

A capacitor has the ability to store electrostatic charge. In an in a conductor, but decays at a low rate depending upon isolated conductor of charge q as shown in Fig. 4, the ratio of the resistivity of the materials and isolated conductor of charge  $q$  as shown in Fig. 4, the ratio of the resistivity of the materials and, in the case of a nonlin-<br>its charge  $Q$  and potential V is defined as the capacitance C: ear resistive material like

$$
C = Q/V \tag{29}
$$

Where *Q* is expressed in coulombs (C) and *V* in volts (V), *C* will be in farads (F).

In the parallel plate capacitor of Fig. 3, the electric field is given by Eq. (17). The total charge Q on each plate is deter- where  $\tau$  is the charge decay relaxation time constant defined

$$
\int_{S} (\epsilon_0 \epsilon_r \boldsymbol{E}) \cdot d\mathbf{S} = \sum q = Q \qquad \tau = \epsilon_0 \epsilon_r \rho \tag{34}
$$

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**Table 2. Volume Resistivity of Different Materials**

 $P$ (*r*)  $P = V/d$ ,

$$
\epsilon_0 \epsilon_{\rm r} \frac{V}{d} A = Q
$$

where *A* is the surface area of each plate. Since

$$
C = Q/V = \epsilon_0 \epsilon_r A/d \tag{30}
$$

or

$$
U = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C}
$$
 (31)

sity of charge. When  $q_v$  is known, this equation can be used<br>to calculate  $V(r)$ . We have assumed  $\epsilon_r$  is independent of the<br>spatial coordinates.<br>cal resistivity of a material,  $\rho$ , is related to the resistance R

$$
\rho = RA/l \qquad (\Omega \cdot m) \tag{32}
$$

where *A* is the cross-sectional area, *l* is the length of the mate-

ohm-meters. The surface resistivity is expressed in ohms per

The volume resistivity varies widely for different materi-

# **Charge Decay**

**Capacitance**<br>A capacitor has the ability to store electrostatic charge. In an in a conductor but decays at a low rate depending upon ear resistive material like polymer powder, the potential across it. The decay of charge  $q_0$  across the dielectric medium of a capacitor can be described by the simple exponential expression

$$
q = q_0 \exp(-t/\tau) \tag{33}
$$

mined using Gauss's law [Eq. (23a)]: as the product of the dielectric constant  $\epsilon_r$  of the material, its resistivity  $\rho$ , and the permittivity of free space,  $\epsilon_0$ :

$$
\tau = \epsilon_0 \epsilon_\text{r} \rho \tag{34}
$$

can easily be measured experimentally. If the dielectric con- meter. In air, when  $E$  exceeds the breakdown voltage  $E<sub>b</sub>$ . stant is known or can be measured, the resistivity can be determined using Eq. (34). will dissipate through air ionization. Therefore, the maximum

The measured resistance of an insulator may be largely surface charge density in air  $(\epsilon_0 = 1)$  is due to absorbed moisture or contaminants on its surface rather than to its intrinsic volume resistivity. Great care should be taken when measuring volume resistivity to avoid surface contamination.

## **Flow of Charge and Current**

of flow of charge: the medium that surrounds the surface. In free space (vac-

$$
i = \frac{dq}{dt} \qquad (A) \tag{35}
$$

$$
i_{\rm t} = i_{\rm i} + i_{\rm p} + i_{\rm e} \tag{36}
$$

For example, in a typical electrostatic powder spray process, powder particles are charged by ions. The total current is due **Energy of Electrostatic Sparks** to electron current, ion current, and charged particle current. In powder coating applications employing corona guns, the If an isolated charged conductive sphere of capacitance *C*, total current is primarily ion current. Corona charging is dis-<br>whose surface potential is *V*, dischar cussed in the next section. spark, then it dissipates more than 90% of its total energy

When current is distributed over a surface, the concept of surface current density *J* (A/m<sup>2</sup>) is important. It is related to  $U = \frac{1}{2}CV^2$  (41) current by

$$
i = -\oiint \mathbf{J} \cdot d\mathbf{A} \qquad (A) \tag{37}
$$

increases the charge  $[Eq. (35)]$ . The total current density is

$$
\mathbf{J} = \sum \mathbf{J}_i = \sum n_i q_i \mu_i \mathbf{E} \equiv \sigma \mathbf{E}
$$
 (38)

 $\vec{E}$  is the applied electric field. The conductivity  $\sigma$  of a medium charge is stable and has positive resistance. is defined by the summation of the products  $n_i q_i \mu_i$ .

From Gauss's law the electric field at the surface of an imagi-<br> **OF CHARGED PARTICLES** nary sphere that contains a total charge  $q$  is given by Eq. **Charging of Materials** (22):

$$
ES = \frac{q}{\epsilon_0 \epsilon_1}
$$

$$
E = \frac{q}{S} \cdot \frac{1}{\epsilon_0 \epsilon_r} = \frac{Q_s}{\epsilon_0 \epsilon} \tag{39}
$$

The charge decay relaxation time is a lumped parameter and where *Q*<sup>s</sup> is the surface charge density in coulombs per square which is nearly equal to  $3.0 \times 10^6$  V/m, the surface charge

$$
Q_s(max) = \epsilon_0 E_b
$$
  
 
$$
Q_s(max) = 3.0 \times 10^6 \times 8.854 \times 10^{-12} \text{ C/m}^2
$$
 (40)  
= 2.65 × 10<sup>-5</sup> C/m<sup>2</sup>

In electrostatic processes, the current is defined by the rate In general, the maximum electric field is determined by uum), the electric field can be increased until field emission of electrons or ions from the surface occurs.

When the electric field between two electrodes in air exceeds the breakdown voltage, the air ionizes, causing ion cur-It is carried by ions, electrons, and charged particles. Thus rent. Depending on the electrode geometry and the voltage the total current  $i_t$  is given by applied to the electrodes, there will be either a sustained corona or a spark. An overview of corona and sparking processes is given later, but the energy involved in an electrostatic sparking process is illustrated below.

whose surface potential is *V*, discharges in air by means of a

$$
U = \frac{1}{2}CV^2 \tag{41}
$$

A spark is generally characterized by the production of a  $i = -\iint J \cdot dA$  (A) (37) A spark is generally characterized by the production of a high concentration of ions (10<sup>16</sup> ions/m<sup>3</sup>) in a short period of time (1  $\mu$ s). This discharged energy is one of three important where the negative sign indicates that current is considered criteria for predicting an explosion in a medium that may conpositive when *dq*/*dt* is positive; that is, the flow of current tain flammable vapor or particulate materials. The other two increases the charge [Eq. (35)]. The total current density is criteria are the concentration of given by summing the current densities of the charge carri- and the concentration of oxidizing agents, such as oxygen in ers: air. For organic solvents, the minimum ignition energy is about 0.3 mJ. Electrostatic hazard control is discussed below in the section so named. One primary difference between spark and corona discharge is that a spark is characterized where  $n_i$ ,  $q_i$ , and  $\mu_i$  are the number density, magnitude of by a negative resistance so that an unstable high current discharge, and mobility of each carrier type *i*, respectively, and charges in a very short time period, whereas a corona dis-

# **Electrostatic Breakdown Field CHARGING OF MATERIALS AND TRANSPORT**

The three most important mechanisms used in charging ma $t$ erials are: (1) corona charging, (2) induction charging, and 0<sup>r</sup> (3) contact charging, or *tribocharging.* Materials can also be charged by nuclear or ultraviolet (UV) radiation, which ejects<br>electrons from the surface, leaving a net charge on it. In this section, we will discuss in detail the three main mechanisms of charging as well as the transport, deposition, and separation of the charged particles according to the applications.

# **Corona Discharge**

Let us consider two electrodes (Fig. 5), one of which is a wire and has a small radius of curvature, placed coaxially inside a cylindrical pipe. The wire is held at a high potential, and the cylinder is grounded. The electric field near the small-radius wire electrode will have a high intensity. Free electrons in this high-intensity field region will be accelerated and move away from the negative central wire toward the grounded cylinder at high velocities because of their high electrical mobility.

When the energy of these electrons is sufficiently high to produce electron–ion pairs upon impact with neutral gas molecules, ionization occurs. This ionization process repeats many times, creating an avalanche of electrons and positive **Figure 6.** A point-to-plane electrode geometry showing negative co-<br>ions in the high-electric-field region called the corona glow. The preakdown of gas. In the c The process is similar for both positive and negative corona to an energy sufficient to ionize neutral gas molecules. The process is discharges except that the directions of motion of ions and repeated many times, causing an avalanche. As the stream of elecelectrons are reversed. trons moves toward the grounded electrode, there are electron attach-

energy electron collision with the molecules is called a corona. grounded electrode along the field lines and collide with particles.<br>The word comes from the Latin word for "crown" and was both negative ions and the charge of their ships during thunderstorms. Most of the radiation is

in the blue and near-UV spectrum.<br>
The avalanche process, shown in Fig. 6 for a point-to-plane<br>
geometry, is governed by the ionizing potential of gases pres-<br>
ent near the small-radius electrode. Some of the requirements<br>

1. The electron energy in electron volts (eV) must be<br>greater than the ionization potential of the surrounding<br>gas. For example, ionization potential for the  $O_2$  mole-<br>and is 19.9 eV. The electron energy must expect thi value to ionize neutral  $O_2$  molecules to  $O_2^+$  ions and elec- $10^{-19}$  J.  $10^{-19}$  J.



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rona breakdown of gas. In the corona region, free electrons accelerate ments to form  $O_2^-$  ions. The negative ions then move toward the The bluish light emitted in this region because of the high-<br>
ergy electron collision with the molecules is called a corona<br>
grounded electrode along the field lines and collide with particles.

- 
- 3. The corona discharge requires a source of *initiating elec-*
- cule is 12.2 eV. The electron energy must exceed this  $\frac{4}{10}$ . The electric field near the small-diameter electrode value to ionize neutral O<sub>2</sub> molecules to O<sub>2</sub> ions and electron with the corona-initiating field. For trons. An electron volt is  $1.6 \times 10^{-19}$  C  $\times$  1 V =  $1.6 \times$  wire-cylinder geometry, Peek's equation (2) gives the

$$
E_{\rm c} = 3 \times 10^6 f(\delta + 3.0 \sqrt{\delta/a}) \text{V/m} \tag{42}
$$

where

- $f =$  roughness factor of the wire electrode (dimensionless)
- $\delta$  = relative air density =  $(T_0/T)(P/P_0)$
- $a$  = radius of the corona wire (m)
- $E_c$  = corona-initiating field (V/m)
- $T_0 = 298$  K
- $T =$  actual temperature  $(K)$
- $P_0 = 1$  atm
- 
- $P =$  actual pressure (atm)

The voltage  $V_c$  required to initiate corona in a wire cylinder geometry can be written as

$$
V_{\rm c} = 3 \times 10^6 a f \left( \delta + 3.0 \sqrt{\frac{\delta}{a}} \right) \ln \frac{b}{a} \text{ V} \tag{43}
$$

where *a* is the radius of the HV wire electrode, and *b* is the radius of the cylindrical electrode.

The above equation shows that  $V_c$  required to initiate corona increases with the wire radius *a*. As *a* decreases, there Figure 5. A wire–cylinder geometry of an electrostatic precipitator. is a corresponding increase of the electric field near the wire.

Therefore, it is possible to initiate corona at a low voltage provided *a* is small and *b*/*a* is also small. For example, in a Corotron, a corona discharge device is used to charge the photoconducting drum surface, the voltage required to initiate and sustain corona is about 10 kV. In a powder coating booth, a voltage of  $-80$  kV to  $-100$  kV is applied to the powder coating gun to sustain corona current.

In powder coating or electrostatic precipitator applications, it is necessary to have a strong electric field near the collecting electrodes for efficient deposition of charged particles. The magnitude of the electric field near the collecting electrode decreases sharply as distance increases between the two elec- where  $\rho$  is the space charge density, and the subscripts e, i, take place. The electric field in a wire–cylinder geometry, in to electron and charged particles, so that the absence of free charges, can be written by solving Laplace's equation. Since  $b$  and  $a$  are both constants for a given electrode geometry (2), then

$$
E(r) = \frac{V}{\ln(b/a)r}
$$
 (44)

the distance *r* from the wire surface when there are no ions results in negative ions. The number of collisions needed for the effect of corona ions is to increase the field near electron attachment depends on the type of present. The effect of corona ions is to increase the field near electron attachment depends on the type of gas, as shown in<br>the cylinder electrode and decrease it near the high-voltage. Table 3. For practical purposes, o the cylinder electrode and decrease it near the high-voltage Table 3. For practical purposes, only a small amount of  $O_2$ , electrode However for a reasonably high space charge the  $H_2O$ , or  $SO_2$  is needed for electron electrode. However, for a reasonably high space charge, the  $H_2O$ , or  $SO_2$  is needed for electron attachment. <br>electric field at a sufficiently large distance r from the wire negative gases provide stable corona current electric field at a sufficiently large distance  $r$  from the wire can be approximated by  $(3)$ 

$$
E = \left(\frac{J}{2\pi\epsilon_0 b}\right)^{1/2} \qquad r \gg a \tag{45}
$$

For a large high-voltage-electrode diameter, the field decreases less sharply with increasing distance from the discharge wire. Therefore, to increase the field near the But the space charge due to the particles is significant; there-<br>grounded electrode, the diameter of the electrode should be fore as large as possible, consistent with corona generation. At very large values of *a*, the second term of the Eq. (42) can be  $\rho$ neglected, so the corona field  $E<sub>b</sub>$  for air is

$$
E_{\rm b} = 3 \times 10^6 \,\text{V/m} \qquad \text{at NTP} \tag{46}
$$

This is the air breakdown field  $E<sub>b</sub>$  at normal temperature **Ion Wind** 

three components: mate relationship can be written as

$$
\rho_{\rm t} = \rho_{\rm e} + \rho_{\rm i} + \rho_{\rm p} \tag{47}
$$

**Table 3. Electron Attachment Probabilities for Different Gases**

Gas	Average No. of Collisions for Attachment
Inert gas	${}^{\circ}$
$N_2, H_2$	$\infty$
$\mathrm{O}_2$	$4 \times 10^3$
H <sub>2</sub> O	$4 \times 10^4$

trodes and as the diameter of the corona wire electrode de- and p represent space charge components contributed by eleccreases. The volume of the corona region also decreases. Be- trons, ions, and particles, respectively. If there are no electrolow a certain limit in the corona region, no avalanche can negative gas ions present, then the space charge will be due

$$
\rho_{\rm t} = \rho_{\rm e} + \rho_{\rm p} \tag{48}
$$

Since electrons have high mobility, the current will be high and sparkover may occur. A sustained negative corona requires the presence of such electronegative gases as oxygen to produce negative ions.

The field is axisymmetrical and is inversely proportional to Collision between electrons and electronegative molecules the distance r from the wire surface when there are no ions results in negative ions. The number of col

The corona current can be expressed as

$$
J = (\rho_e b_e + \rho_i b_i + \rho_p b_p)E \qquad (A) \tag{49}
$$

where the *b*'s represent the mobilities of electrons, ions, and where *J* is the corona current per unit length of the wire. This<br>approximate value of *E* is independent of *r*. Similarly, in a<br>point-to-plane geometry, the field *E* is approximated by a<br>value between  $V/d$  and  $2V/d$ , w

$$
J = (\rho_e b_e + \rho_i b_i)E \qquad (A) \tag{50}
$$

$$
\rho_{t} = \rho_{i} + \rho_{p} \tag{51}
$$

since each charged particle contains large numbers of unit charges.

and pressure (NTP). Note that in vacuum there can be no<br>corona discharge. The field can be increased, often by two or-<br>ders of magnitude (to  $10^8$  V/m), when field emission of elec-<br>trons or ions from the high voltage el

Generally, corona initiation begins with a rapid current **Electron Attachment by Gas Molecules** jump from nearly zero to a few microamperes. The current When a corona initiates, the total space charge density,  $\rho_t$  has then rises with increasing voltage; in accordance the approxi-

$$
\rho_t = \rho_e + \rho_i + \rho_p \tag{52a}
$$

where  $K$  is a constant depending upon the geometries involved in the corona process,  $V$  is the applied voltage, and  $V_c$ is the corona-initiating voltage. For a point-to-plane geometry, the current density  $J(A/m^2)$  at the surface can be written as

$$
J = KV(V - V_c)/d^2 \tag{52b}
$$

where *d* is the perpendicular distance between the point and the plane electrode. The current density changes as the distance between the point electrode and target surface varies. *J* also varies with time as particles are deposited on the target and the particle cloud density changes in the interelectrode space. ers, and deposition of charged powder on a grounded

used to charge particles or surfaces. For example, the photolating surface, the ions deposit on the surface following the of  $Q_s$ ,  $t$ , and the dielectric breakdown strength (4). Table  $\theta$  field lines. The maximum charge density is limited by the ion-<br>shows the breakdown field fo field lines. The maximum charge density is limited by the ionization of the air surrounding the surface. In air, the breakdown field intensity  $E_b$  cannot exceed  $3 \times 10^6$  V/m. The maxi-

$$
E_{\rm b} = \frac{Q_{\rm s}}{\epsilon_0} \tag{53}
$$

field lines are perpendicular to the surface with magnitude low the electric field lines that terminate on the particle, and  $E = Q_s/\epsilon_0$  independent of the distance from the surface:

$$
Q_{\rm s}(\text{max}) = E_{\rm b}\epsilon_0
$$
  
= 2.64 × 10<sup>-5</sup> C/m<sup>2</sup> (54)

thickness  $t$ , there will be a breakdown voltage setting the maximum surface charge limit of capacitors:

$$
Q_{\rm s} = CV_{\rm s}
$$

$$
V_{\rm s} = \frac{Q_{\rm s}t}{\epsilon_0 \epsilon_{\rm r}}\tag{55}
$$

where *t* is the thickness of the insulating layer between the cle,  $\epsilon_r = 1$ ,  $p = 1$ .<br>two conducting plates and  $Q_s$  is the surface charge density. The charge-to-mass ratio of a spherical particle of density two conducting plates and  $Q_s$  is the surface charge density. The charge-to-mass ratio of For a dielectric film or a powder layer on a conducting plate.  $\rho_s$  can be calculated as follows: For a dielectric film or a powder layer on a conducting plate, the surface voltage is thus limited by  $t$  and  $\epsilon_r$ . In typical applications related to copying machines or laser printers, the surface voltage is of the order of 600 V for  $t = 20 \mu m$  and  $\epsilon_r = 3$ .

When charges accumulate on an insulating layer backed by a grounded metal plate, image charges develop across the dielectric film, forming a capacitor. Under such conditions, the field *E* external to the charged layer is almost zero, since where  $d_n$  is the particle diameter, and  $(q/m)_{\text{max}}$  is the maxithe entire field becomes bound between the charged surface mum charge-to-mass ratio in an electric field *E* in a corona layer and its image charges across the dielectric film. A por- charging process. tion of the accumulated charge may leak through the film. For a spherical particle, the maximum charge-to-mass rastatic precipitators, optical photoconductor operation in print- not depend on the density of ions.

**ELECTROSTATIC PROCESSES 23**

	Migration Velocities for Particles with Maximum Charge		
Particle	Terminal Settling	Terminal Electrical	
Diameter	Velocity	<b>Migration Velocity</b>	
$(\mu m)$	$\rm (cm/s)$	$\text{(cm/s)}$	
0.2	0.0002	1	
$\boldsymbol{2}$	0.013	10	
20	$1.2\,$	100	
100	25	500	
200	70.8	1000	

**Table 4. Comparison of Terminal Settling and Electrical Migration Velocities for Particles with Maximum Charge**

**Corona Charging of Substrates and Particles** the the thin insulating workpiece in a powder coating process. Here the the thin insulating layer acts like a distributed capacitor. De-**Substrate Charging.** Ions from a corona discharge can be pending on the film thickness, a considerable amount of ed to charge particles or surfaces. For example, the photo-<br>charge density, often in excess of the limit set conducting surface of an optical photoconductor (OPC) in a may be present and lead to back corona, dielectric breakdown, copying machine is charged by corona discharge. For an insu-<br>and propagating brush discharge, dependi copying machine is charged by corona discharge. For an insu-<br>lating surface are discharge in the surface following the of  $Q_s$ , t, and the dielectric breakdown strength (4). Table 4

Particle Charging. A particle placed in an electric field is mum surface charge density  $Q_s$  at the breakdown point is polarized and therefore attracts ions of both polarities. In an obtained from electric field containing unipolar ions and uncharged particles, the particles will acquire charge of one polarity due to the local deformation of the electric field. Similarly, a charged particle can be neutralized in a biionized field. The electric field is distorted by the presence of the particles, and as the For an isolated large flat surface with charge density  $Q_s$ , the particles acquire charge, the distortion changes. The ions fol-<br>field lines are perpendicular to the surface with magnitude low the electric field lines that charging continues until the retained charge on the particle repels additional ions. Saturation charge occurs when the attractive field due to field distortion equals the repulsive field due to the charge on particles. This charging process is known as *field charging.* For a spherical particle of radius *r* in an For a parallel plate capacitor of dielectric constant  $\epsilon_r$  and electric field *E*, the maximum charge limit is known as the thickness *t*, there will be a breakdown voltage setting the Pauthenier limit, first derived by

$$
Q_{\text{max}} = 4\pi\epsilon_0 r^2 pE \tag{56}
$$

where *r* is the particle radius,  $p = 3\epsilon_r/(\epsilon_r + 2)$ ,  $\epsilon_r$  is the dielectric constant, and *E* is the electric field. For a conducting particle one has  $\epsilon_r = \infty$ ,  $p = 3$ , and for a highly insulating parti-

$$
m = \frac{4}{3}\pi r^3 \rho
$$
  

$$
\frac{q_{\text{max}}}{m} = \frac{4\pi \epsilon_0 r^2 p E}{\frac{4}{3}\pi r^3 \rho_p} = \frac{3\epsilon_0 p E}{\rho_p r} = \frac{6\epsilon_0 p}{\rho_p d_p} E
$$
(57)

This leakage depends upon the resistivity of the film or pow- tio (1) varies linearly with *E*; (2) varies inversely with the der layer. Examples are charged fly ash deposition in electro- particle diameter  $d_p$ , (3) is a weak function of  $\epsilon_p$ , and (4) does

The density of ions influences the time it takes for a parti- or cle to reach its saturation charge. The charge on a particle at any time *t* is given by

$$
q = q_{\text{max}} \frac{1}{1 + \tau/t} \tag{58}
$$

saturation charge and is given by

$$
\tau = 4\epsilon_0 / N_0 e b \tag{59}
$$

where  $N_0$  is the ion density (ions/m<sup>3</sup>), b is the mobility of ions, charge at  $t = \tau$  and 95% of its saturation during the time period  $3\pi$ .  $F_g = mg = \frac{4}{3}$ 

The electrical mobility *Z* is the velocity of a charged particle in an electric field of unit strength and is related to the elec-  $d_p < 100 \mu m$ ) as trical migration velocity  $V_e$  of a particle in a field  $E$  by

$$
V_{\rm e}=ZE
$$

$$
Z = V_e/E \tag{60}
$$

$$
Z = q/3\pi \eta d_{\rm p} \tag{61}
$$

where  $\eta$  is the viscosity of the medium and  $d_{\nu}$  is the diameter of the particle. the electrostatic forces can be made to dominate both gravita-

The electrostatic force on charged particles free to move in <sup>a</sup> dielectric medium will soon attain a terminal electrostatic **Back Corona** migration velocity when the driving force *qE* becomes equal to the drag resistance force. The electrostatic force on a parti-<br>Back corona is the ionization of powder deposited on a con-

$$
F_{\rm e} = qE \tag{62}
$$

valid (particle motion at small Reynolds number  $Re_p < 1$ ), can back corona. The continuous bombardment of the powder be written with ions can cause the field strength to exceed the break-

$$
F_{\rm d} = 3\pi \eta d_{\rm p} V_{\rm e} \tag{63}
$$

suming the particle is charged to the Pauthenier limit in an down. Eventually a point is reached when the back corona electric field  $E$ , the surface charge density is  $Q_s$  and is given prevents further deposition. by When back corona at the deposited, negatively charged

$$
Q_{\rm s}=q/4\pi r^2
$$

$$
Q_{\rm s} 4\pi r^2 E = 6\pi \eta r V_{\rm s}
$$

$$
V_{\rm e} = \frac{qE}{6\pi\eta r} = \frac{Q_{\rm s}d_{\rm p}E}{3\eta} \tag{64}
$$

Equation  $(64)$  shows that when particles are charged to their saturation limit, the electrical migration velocity is directly where  $\tau$  is the time taken by the particle to reach one-half the proportional to the diameter of the particle and the electric seturation charge and is given by

For example, if the electric field is  $10^5$  V/m, then the electrical migration velocity  $V_e \approx 10$  m/s for a particle diameter  $d_p = 200 \mu m$ ,  $V_e \approx 1 \text{ m/s}$  for  $d_p = 20 \mu m$ , and  $V_e \approx 10 \text{ cm/s}$ where  $N_0$  is the ion density (ions/m<sup>3</sup>), *b* is the mobility of ions, for  $d_p = 2 \mu m$ . We can compare these velocities with the graviand *e* is the electronic charge. The particle acquires 50% of its tational settling v tational settling velocities for particles of different sizes, since

$$
F_g = mg = \frac{4}{3}\pi r^3 \rho_p g \tag{65}
$$

**Electrical Mobility**<br>
The particles reach terminal settling velocity when  $F_g = F_d$ .<br>
The terminal settling velocity  $V_{TS}$  can be approximated (for

$$
V_{\rm TS} \approx 0.003 d_{\rm p}^2 \,\rm cm/s \tag{66}
$$

where  $d<sub>v</sub>$  is in micrometers. The examples in Table 4 show that  $V_e$  can be much larger than  $V_{TS}$ .<br>Clearly, the electrical migration velocity for particles up

to a certain diameter (approximately 24 mm) charged to the Pauthenier limit is much larger than the gravitational set-For a spherical particle of charge  $q$  and moving in a uniform thing velocity. The electrical migration velocity increases linearly with the diameter  $d$ , whereas the settling velocity increases with the square of the diameter  $(d^2)$ . However, the *z* electrical migration velocity for small particles is often negligible compared to the aerodynamic forces in a turbulent air flow field. For particles in the size range 1  $\mu$ m to 1000  $\mu$ m, tional and aerodynamic forces in applications related to elec-**Electrical Migration Velocity** trostatic precipitators, electrostatically charged filters, pow-<br>der coating, and charge separators.

cle of charge  $q$  in an electric field  $E$  can be written ducting substrate due to a high electric field across the powder layer. Back corona plays an important role in electrostatic *<u>Ferrerigitation</u>* and in powder coatings, and occurs when powder has high resistivity. Even a monolayer of highly resistive The drag force  $F_d$  on the particle, assuming Stokes's law is powder deposited on the conducting substrates can produce down field strength of air ( $E_{\rm b}$  = 3  $\times$  10 $^{\rm 6}$  V/m) a few seconds after deposition begins. The deposition rate on the surface of the workpiece rapidly decreases because of the back corona, where  $V_e$  is the particle velocity relative to the medium. As- causing the thickness buildup of the powder layer to slow

powder layer occurs, positive ions start migrating toward the *negative-corona gun electrode. This stream of positive ions* will neutralize the oncoming negatively charged particles, ad-When  $F_e = F_d$ , we have the terminal electrical migration ve-<br>locity<br>corona. Since back corona occurs randomly on the surface it corona. Since back corona occurs randomly on the surface, it produces a random variation of film thickness. At each point *<sup>Q</sup>*s4π*<sup>r</sup>* of back corona initiation, there is an eruption of powder from <sup>2</sup>*<sup>E</sup>* <sup>=</sup> <sup>6</sup>πη*rV*<sup>e</sup> powder charging. Under severe back corona, the intensity is der surface condition. sufficiently strong to fuse the powder particles where the If the workpiece surface has protuberances, the electrical breakdown occurs. Back corona causes the powder film to ap- field intensifies at those points and breakdown will occur pear ''spot-welded'' all over the surface, resulting in tiny cra- there first. Therefore, surface irregularities, including sharp ters, pinholes, and an orange-peel appearance after curing. In edges, strongly influence the occurrence of back corona. general, back corona limits the efficiency of the electrostatic deposition of powder and it alters the appearance of the film **Diffusion Charging**

- 
- 
- 
- 
- 4. Results in overspray of powder within a few seconds.<br>5. Decreases the deposition rate in those areas where<br>5. Decreases the deposition rate in those areas where<br>there is a sufficient powder buildup. However, the depo-<br> sition rate remains high where there is no back ioniza-<br>tion and the layer thickness is low. Thus, the buildup of  $(\text{ions/m}^3)$ , it will acquire in time *t* charge  $q(t)$  given by the powder layer across the entire surface is a self-limiting process resulting in a fairly uniform thickness of powder film.
- 
- layer to approximately  $5 \times 10^6$  V/m. Therefore, for a

$$
E_{\rm b} = \frac{V_{\rm d}}{d}
$$
  
\n
$$
V_{\rm d} = 5 \times 10^6 \times 100 \times 10^{-6} \,\rm V
$$
  
\n= 500 V

$$
V_{\rm d} = J \rho t \tag{67}
$$

$$
J = E/\rho \qquad (A/m^2) \tag{68a}
$$

$$
J = \frac{5 \times 10^6 \text{ V/m}}{10^{15} \Omega \cdot \text{m}} = 5 \times 10^{-9} \text{ A/m}^2
$$
 (68b)

This current density is much smaller than the forward corona Another method of generating bipolar ions uses radioactive density of  $10^{-4}$  A/m<sup>2</sup> in an electrostatic precipitator. It signi- sources such as krypton-85 ( ${}^{85}$ Kr) and polonium-210 ( ${}^{210}$ Po). fies that ion currents higher than this value will lead to a Radioactive sources generate bipolar ions, which can neutralground or are being deposited on the powder layer, increasing sources is that no high voltage is necessary and hence they the surface charge. This shows that the volume conduction of can be used where electrostatic sparks would be a serious current through the powder is relatively small, meaning back hazard. However, the management of radioactive sources

the surface because of the breakdown and polarity reversal of corona is influenced more by the interstitial air and the pow-

in a powder coating process.<br>In summary, back corona: particles larger than  $2 \mu m$  in diameter, diffusion charging becomes important for particles smaller than  $1 \mu m$  in diameter. 1. Occurs when high-resistivity fly ash or polymer powder<br>deposits on a surface, causing the electric field across<br>the powder layer to exceed the breakdown voltage of the<br>cinca between the thermall movides and the ions an the powder layer to exceed the breakdown voltage of the signs between the small particles and the ions. In a corona<br>dielectric medium surrounding the powder layer.<br>2. Creates ions of opposite polarity, which discharge the Creates ions of opposite polarity, which discharge the all particles, but as mentioned, field charging predominates powder and disrupt the deposition process. for large particles and diffusion charging for small ones. In 3. Rapidly decreases the efficiency of the powder deposi- the intermediate range, both processes contribute signifition.<br>
For the absence of an electric field and where unipolar<br>
Results in overspray of powder within a few seconds<br>
ions are present, the charging is only by the diffusion process.

$$
q(t) = \frac{4\pi\epsilon_0 rkT}{e} \ln\left(\frac{rN_0e^2ut}{4\epsilon_0 kT} + 1\right)
$$
 (69)

6. Causes pinholes, moon craters, and orange peels in the where r is the particle radius, k is Boltzmann's constant, T is the discussed film.<br>The absolute temperature in kelvin, e is the electronic charge,<br>T. Limits the e and  $u$  is the mean thermal speed of ions (approximately 240) layer to approximately  $5 \times 10^6$  V/m. Therefore, for a  $m/s$ ). If the ions have more than one electric charge, *e* should film thickness of 100  $\mu$ m, the voltage drop will be given be replaced by *n*, the ionic charge Di film thickness of 100  $\mu$ m, the voltage drop will be given be replaced by  $n<sub>1</sub>$ , the ionic charge. Diffusion charging will by continue until the electric field due to the surface charge of the particle exceeds the ionization potential of the gas.

Diffusion charging is extensively used for submicron particles. For example, in an electrical mobility analyzer, the ultrafine particles are charged with unipolar ions with single electronic charge and then analyzed according to their electrical mobility *Z*. Size classification of ultrafine particles is pos-Here sible using a mobility analyzer.

# $Charge$  **Neutralization**

Where  $J$  is the current density,  $\rho$  is the resistivity of the neutralization of electrostatic charge on computer chips using powder layer, and  $t$  is the film thickness; we have hipolar ions of high concentration. Bipo using a corona discharge device driven by an ac voltage, usually 5 kV at a frequency of 60 Hz (4). Both positive and negative corona discharges are generated by using wire–cylinder For a powder resistivity of  $10^{15} \Omega \cdot m$ , electrode geometry. The positive and negative ions discharge the electrostatic charge on insulating or semiconducting sur- $J = \frac{5 \times 10^6 \text{ V/m}}{10^{15} \Omega \cdot \text{m}} = 5 \times 10^{-9} \text{ A/m}^2$  (68b) faces where electrostatic charge neutralization is necessary.<br>This type of ionizer is extensively used in semiconductor industries.

condition where excess ions either are finding a path to ize charged particles or surfaces. An advantage of radioactive



**Figure 7.** Induction charging of a spherical conducting particle that enters the electric field between two parallel plates and bounces off the grounded electrode with a net negative charge. **Figure 9.** At the left is shown a discharged gold-leaf electroscope. In

lations that apply to nuclear radiation. <br>a switch neutralizes the positive charge. If the grounding is discon-

Induction charging is illustrated in Fig. 7. A spherical con-<br>ducting particle that enters an electric field between two par-<br>allel plates experiences induction charging. At position A the charging time to be 0.1 ms or le particle's surface charge is uniformly zero. At *B*, negative charges are induced in areas close to the top positive plate, and the induced positive charges are repelled furthest from

Induction charging requires that the surface or volume<br>conductivity of the material be high enough for charge leak-<br>age to occur before separation of the object from the electrode<br>(5). The time constant for the leakage of mated from the charge relaxation time  $\tau = \epsilon_0 \epsilon_r \rho$ . Since  $\epsilon_0$  =  $8.854 \times 10^{-12}$  F/m, the resistivity  $\rho$  should be less than  $10^{10}$ 



the middle a charged sphere is brought near and induction charging occurs. Bound charges are at the top of the electroscope, and free must be carried out according to the strict health safety regu- charges are on the leaves at the bottom. Grounding the sphere using nected and the charged sphere is moved far away, the entire electroscope becomes negatively charged. **Induction Charging**

$$
\rho = \frac{10^{-4} \,\mathrm{s}}{8.854 \times 10^{-12} \times 80} \,\Omega \cdot \mathrm{m} = 1.4 \times 10^{11} \,\Omega \cdot \mathrm{m} \tag{70}
$$

the positive plate. Once the ball touches the grounded plate<br>
at point  $C$ , the free positive charge leaks to the ground, leav-<br>
ing the bound induced negative charge. See the positions  $D$  and<br>  $E$ , the spherical conduct



fiber. the ring electrode.



**Figure 8.** Induction charging of a metal fiber where the bound **Figure 10.** Induction charging of a conducting liquid. As the droplet charges were neutralized, leaving charges of same polarity of the leaves the nozzle, it carries charge with a polarity opposite to that of

particle will polarize and move in the direction of the convergence of the electric field. This phenomenon is known as dielectrophoresis.

# **Triboelectric Charging**

Tribocharging occurs through two mechanisms: (1) contact charging and (2) friction charging. In both cases, the mechanical processes that produce the charging of materials are: (a)sliding, (b) rolling or milling, (c) impact, (d) vibration of the<br>surface at contact, (e) separation of solid–solid, solid–liquid,<br>and fully occupied bands at 0 K. For an insulator, the conduction<br>and liquid–liquid surface pends upon their relative speed and on the pressure between energy states that are partially full. them. As the pressure increases, the area or the number of contact points increases. The surface charge density achieved by this process can be very high, up to  $2 \times 10^{13}$  e/m<sup>2</sup> maximum surface charge density the average distance be- nm. Thus we have tween two charged atoms is only about 10 interatomic distances. Surfaces reaching the saturation charge level, however, contain no more than 8 to 10 electronic charges per million surface atoms.

**Contact Charging.** Contact charging between two surfaces The charge exchange is very rapid in metals; therefore, does not require relative motion between them. The two surfaces upon separation, the two surfaces are practi

There is a wealth of literature available on the contact<br>charging process, but the experimental results are often con-<br>tradictory and sometimes confusing. Two models that are<br>most commonly used to explain contact charging the electrostatic charging models in the light of their own work and that of other researchers such as Chowdry and Westgate (9), Harper (10), Krupp (11), Duke and Fabish (12), and Schein and Cranch (13). where  $C_M$  is the capacitance between the metal and insulator

ent work functions,  $\phi_A$  and  $\phi_B$ , are in contact, electrons tunnel Fermi levels  $\phi_{M1}$ ,  $\phi_{M2}$ , ..., and then plot *Q* versus  $\phi_M$ , the from one surface to the other. The potential difference at the intercept will indicate the value of  $\phi_1$  when  $Q = 0$ . For metals, point of contact can be written as (6), the work function  $\phi_M$  can be plotted against a standard metal

$$
V_{\rm C} = \frac{\phi_B - \phi_A}{e} \tag{71}
$$

$$
Q = C_{AB} V_C \tag{72}
$$

between the surfaces. the energy levels close to the metal's Fermi level  $\phi_M$ .

verse flow of electrons takes place by tunneling. The tunnel- electronic energy states are filled. For an insulator, the sur-



**ELECTROSTATIC PROCESSES 27**



chanical discontinuities of the surface wave function provide surface

ing stops when distance between the two surfaces exceeds 1

$$
Q = C_0 \frac{\phi_B - \phi_A}{e} \tag{73}
$$

where  $C_0 = C_{AB}$  at  $d = 1$  nm.

$$
Q = C_{\rm M1} \frac{\phi_{\rm M} - \phi_{\rm I}}{e} \tag{74}
$$

surfaces. If we vary  $\phi_M$ , that is, if we measure the exchange **Metal–Metal Contact Charging.** When two metals of differ- of charge *Q* between the insulator and different metals of like gold. A linear relationship is expected. However, for many insulators linear relationships are not observed (6).

Fabish et al.'s (6) experiments showed that for contacts between an insulator and a metal, the insulator's surface gains and the charge exchanged by tunneling between the two con-<br>tacting surfaces can be expressed as<br>tor. The researchers explained the tribocharging of the insula-<br>tor. The researchers explained the tribocharging of the insula tor using the following model. The insulator has a range of *localized energy levels* (molecular-ion states), with a spread of 0 to 5 eV, caused by molecular vibration; furthermore, the where  $V_c$  is the contact potential and  $C_{AB}$  is the capacitance charge exchange can occur only within a narrow window of

When the two metals are separated from each other, re- An important property of contact charging is how these

face energy states are often partly filled. Schein (6) estimates that  $10^{12}$  to  $10^{15}$  energy states per square meter per electron volt may be involved in explaining some of the experimental data reported in the literature.

The ion-exchange process involves transfer of counterions from the powder (toner) surface to the surface of another material (carrier) with which the powder comes into contact. In summary, the driving forces and controlling parameters involved in the electrostatic contact charging process are:

- 1. The nature of the charge carrier (electrons or ions)
- 2. The difference in work function
- 3. Tunneling mechanisms
- 4. The energy states involved (surface or bulk, extrinsic or intrinsic)
- 5. The surface state densities
- 6. The type of contact, contact area, and friction involved
- 7. Particle–particle charging

In order to understand the charge transfer, it is necessary to **Figure 12.** Contact charging of coal against a metal surface. understand the electronic surface energy structure of the materials. terms of additional electrons in the conduction band (*n*-type)

*tor* has a large forbidden energy gap, up to 12 eV. A much **Electrostatic Charging of Polymers** higher temperature is required to move electrons to the conduction band from the valence band. A *semiconductor* is also Polymer particles under dry conditions and at a low relative an insulator at a low temperature. Its forbidden energy gap is humidity are insulators with resistivity approximately  $10^{14}$ on the order of 1 eV. At room temperature, there are sufficient  $\Omega \cdot m$ . For insulators that are partly amorphous, the lattice numbers of electrons in the conduction band. A semiconductor structure is disordered and there are localized energy levels or an insulator may contain impurity atoms. The impurity within the bandgap of the insulator, due both to the discontiatoms can give rise to additional energy levels, either in nuities in the normal structure of the material at the surface,



Energy Bands. In an isolated atom, each electron has a or holes in the filled valence band (*v*-type). These charge currequentum of energy, Bms defined orbits around the nueleus of riens permit the conduction of current (

and to the presence of impurity atoms. Both structural discon- transfer: (1) low surface density and (2) high surface density. tinuities and the impurity atoms at the surface contribute to In the first case, the number of charges exchanged between the intrinsic and extrinsic surface states. the metal and the insulator is equal to the number of surface

the number of surface atoms; however, because of the maxi- metal and insulator does not cause a significant shift in the mum charge in a given environment, the actual density of the insulator energy levels. In contrast, in the limit of high sursurface states active in a charge transfer process is much face density, as the large number of surface states get filled, lower, generally in the range of 1 to 10 surface states per there is a strong electric field between the metal and insulamillion surface atoms. Since there are approximately 2  $\times$  $10^{19}$  atoms/m<sup>2</sup>, the surface state density generally ranges which limits further charge transfer (3). Until very recently, from  $10^{12}$  m<sup>-2</sup>  $\cdot eV^{-1}$  to  $10^{15}$  m<sup>-2</sup>  $\cdot eV^{-1}$ . It follows that surface impurity levels of few parts per million can significantly alter metal–insulator charging processes; however, Schein (6) has the nature of surfaces states and therefore the polarity and shown that, particularly for toners, the charge transfer data magnitude of electrostatic charge that an insulator surface can be better explained assuming the high-surface-density can acquire. Since no real surface can be clean unless it is limit where the interfacial electric field controls the charge under an ultrahigh vacuum, physisorption and chemisorption transfer process. of contaminants by surface atoms influences the electronic surface structure of the insulator and the resulting electro- **Ion Transfer** static charging. Often, these uncontrolled surface properties<br>often lead to unpredictable electrostatic charging.<br>In the ion transfer model,  $u_i$  represents a chemical potential.<br>Ion transfer depends upon the difference i

In metal–insulator contact charge exchange, different metals after contact as deplete or fill the surface states of the insulator, depending upon the position of the *surface work function* of the insulator with respect to the Fermi level of the metal. There are a number of external factors involved in contact charging under ambient conditions. First, there is a metal oxide layer, which is where  $N_i$  is the surface density of ions, and  $u_1$  and  $u_2$  are the always present when a metal is exposed to air. Second, the potential energies of the two surfaces or their affinities for particles are also often coated with an oxide layer and other the ions in the ions transfer process, respectively. contaminants. The contact charge exchange density  $\sigma$  on the Real surfaces are always covered with adsorbed layers,

$$
\sigma = eN_{\rm s}(\phi_{\rm i} + \Delta E - \phi_{\rm m})\left(1 + \frac{e^2 N_{\rm s} d}{\epsilon}\right)^{-1} \eqno(75)
$$

the Fermi level of the metal surface,  $\Delta E$  is the energy gap created by the oxide layer,  $N_s$  is the surface state density per unit area per unit energy (eV), *e* is the electronic charge, *d* is **FRICTION CHARGING** the thickness of the oxide layer, and  $\epsilon$  is the permittivity of the oxide layer. In the limit of low surface state density, In addition to the contact process, temperature differences be-<br> $e^2N_s d/\epsilon \ll 1$ , and if we include a factor f to represent the frac-<br>tween the contact points are

$$
\sigma = f \epsilon N_s (\phi_i + \Delta E - \phi_m) \tag{76}
$$
\n
$$
q \propto F^a \tag{79}
$$

In the limit of high surface state density,  $e^2 N_s d/\epsilon \geq 1$ , Eq. (75)

$$
\sigma = f \epsilon \frac{\phi_{\rm i} + \Delta E - \phi_{\rm m}}{ed} \tag{77}
$$

The above expressions show that contact charging depends upon the surface oxidation and on the density of the surface states. The physical meaning of  $\phi_i$ , the surface work function of an insulator, is not clearly established, nor is it known how surface states are distributed within the forbidden energy gap where  $K_1$  and  $K_2$  are constants depending upon the mechaniof the insulator. cal properties of the materials (Poisson's ratio and Young's

are often considered in the surface state theory of charge coming speed,  $d_p$  and  $p_p$  are the particle diameter and density,

Theoretically, the number of surface states can be equal to states, and is low enough that the electric field between the tor, raising the energy levels of the insulator surface states, the low-density limit was considered to be the case for most

contacting surfaces for specific ions. Harper's model, as dis- **Electron Transfer** cussed by Schein (6), estimates the surface charge density

$$
\sigma_{\rm s} = N_{\rm i} \exp\left(-\frac{u_1 - u_2}{kT}\right) \tag{78}
$$

insulator can be expressed as (7) which are frequently ionic in nature, or contain a charged double layer. An adsorbed water layer 10  $\mu$ m thick will be a substantial potential barrier to the transfer of electrons. However, ion exchange can take place across the contacting double layer. Direct observation of ion transfer in contact charging where  $\phi_i$  is the surface work function of the insulator,  $\phi_m$  is between a metal and a polymer has been reported in the liter-<br>the Fermi level of the metal surface  $\Delta F$  is the energy gap ature (6).

tion of geometric area that makes intimate contact, then Eq.  $\frac{1}{2}$  factor in tribocharging. The exchange of charge (q) can be re-<br>(75) can be approximated as  $\frac{1}{2}$ 

$$
q \propto F^a \tag{79}
$$

In the finit of high surface state density,  $e^{j}$   $\mathbf{v}_s u \in \mathbb{R}^d$ ,  $\mathbf{v}_s u \in \mathbb{R}^d$ ,  $\mathbf{v}_s u \in \mathbb{R}^d$ , where *a* is a factor (0.3 to 1) that depends upon the type of contact.

Gidaspow et al. (14) considered the impact velocity *V* and computed the charge exchange following a model developed by Chang and Soo:

$$
Q = K_1 K_2 |V|^{0.6} d_p^2 \rho_p^{0.8} (\phi_i - \phi_m) \frac{N_i N_m}{N_i + N_m}
$$
 (80)

Equations (76) and (77) show the two limiting cases that modulus) and upon the ratio of the rebound speed to the in-

*V* is the velocity,  $\phi_i$  and  $\phi_m$  are the work functions of the insu- travel from the high-voltage wire electrode to the cylinder or

to generate negative corona. Negative voltage is applied stream by the electric field.<br>The electrical migration velocity of the charged particle in



cipitator. gas flow is considered laminar. However, in most precipita-

lator and metal, respectively, and  $N_i$  and  $N_m$  are the corre- to the parallel plates. During their passage along the field sponding surface state densities.  $\qquad \qquad$  line, the ions deposit on the particles. In most cases, the particles reach their saturation charge during their transit **ELECTROSTATIC PRECIPITATORS** brough the precipitator, and because of the electrostatic field and image forces, particles deposit on the surfaces of the col-The alectrosteric precisions was the first major interaction later-dedred interaction. The results are the first major interaction interactions were demonstrated into the constrained interaction of the constrained in the

an electrostatic precipitator, under an idealized condition, is given by (4)

$$
W = \frac{qEC_{\rm C}}{3\pi\mu d_{\rm P}}\tag{81}
$$

where *W* is the migration velocity of particles of diameter  $d_{P}$ ,  $\eta$  is the viscosity of a gas, *E* is the electric field, and  $C_{\text{C}}$  is the Cunningham slip correction factor. The above equation de-**Figure 13.** Wire–plate electrode geometry used in an industrial pre- scribes the particle motion in an idealized condition where the tors the gas flow is turbulent. The particles arrive near the boundary layer of the collecting wall by the turbulent motion of the fluid flow. When charged particles are close to the wall, electrostatic attraction forces become effective for their deposition. Using this turbulent model, Deutsch derived the collection efficiency (CE) as follows:

$$
\mathrm{CE} = 1 - \exp(-W_{\mathrm{E}}S_{\mathrm{C}}/Q_{\mathrm{G}}) \tag{82}
$$

where  $W_{\rm E}$  is the effective migration velocity (m/s),  $S_{\rm C}$  is the total collection area (m<sup>2</sup>), and  $Q_{\text{G}}$  is the gas flow rate (m<sup>3</sup>/s). The effective migration velocity is based upon the turbulent flow model. Deutsch's equation does not include nonlinear effects. Modification of this equation is therefore necessary, because several nonlinear factors, including corona quenching, variation of space charge, back corona, and a high-resistivity dust layer, are present in an actual precipitator.

The major components of an electrostatic precipitator are:

- 1. *High-Voltage Supplies.* Power supplies usually range up to  $-100$  kV. The current capacity depends upon the total surface area of the precipitator. A typical ion current concentration on the collector plates is  $10^{-4}$  A  $\cdot$  **Figure 14.** Induction charging of conductive droplets produced by m<sup>-2</sup>. From the collector plate design, the current capac-<br>ultrasonic excitation. ity for each power supply is determined.
- 2. *Corona Charging Sections.* In most industrial electrostatic precipitators, charging and precipitation are per-<br>formed by the same electrodes. For residential applica-<br>tion, a two-stage precipitator is used, where the dust<br>particles are charged in the charging section and are used, primarily for two reasons: (1) negative corona is
- 
- surface of the electrodes.
- 5. *Gas-Handling Device*. Used to move the dust-laden gas into the precipitator, and move the clean gas from the

There are two basic ink jet printing (4) mechanisms: (1) dropon-demand and (2) continuous. In the drop-on-demand process, each drop is produced on demand (i.e. when needed on<br>the target surface) by the application of pulsed energy—<br>thermal or piezoelectric. In the continuous process, a high-<br> $\frac{1}{2}$  and  $\mu$ s, the jet velocity  $U_j$  c pressure jet is used to produce a fine stream of liquid. The nozzle, usually with diameter 35  $\mu$ m, is vibrated at a fre-



most industrial precipitators, negative high voltage is verted at high speed to the desired spots on the target for<br>used primarily for two reasons: (1) perstine corons is printing. When the droplets are not needed, the pow more stable, and (2) one can operate the negative corona plies to both the charging and deflection electrode systems are<br>at a much higher veltage than a positive corona. Noge turned off and the uncharged and undeflected in

at a much higher voltage than a positive corona. Nega-<br>turned off and the uncharged and undeflected ink drops are<br>tive corona produces more ozone than positive corona,<br>and since ozone is a health hazard, negative corona i

$$
\frac{\pi d_{\rm j}^2 \lambda}{4} = \frac{\pi d_{\rm a}^3}{6} \tag{83}
$$

precipitator to a discharge stack or to another device for  $\lambda$  is also called the surface wavelength. Krein and Robinson give the following relationships (4):

**INK JET PRINTING** 
$$
\lambda = 4.5 d_j \tag{84}
$$

$$
d_{\rm d} = 1.89 d_{\rm i} \tag{85}
$$

$$
U_j = \lambda / t_\text{d} = 4.5 d_j / t_\text{d} \tag{86}
$$



be about 35  $\mu$ m; therefore,  $U_j$  is 15.75 m/s. A static pressure workpiece, (2) the coulombic repulsive force between particles as high as 470 kPa is often used to force ink through a jet of arriving at the substrate an diameter 38  $\mu$ m. An experimental arrangement of an ink jet with the same polarity, (3) van der Waals forces, and (4) force printer is shown in Fig. 15.

During the formation of the droplets, small satellite drop-<br>lets are also formed. Usually, it is desired to operate the jet the particles onto the workniece until the coating is cured in without forming satellites, which is possible by adjusting  $t_d$  the oven. and  $\lambda/d_d$ . Approximately 300 V is applied to the cylindrical electrode to charge droplets to near saturation with a charge-<br>to-mass ratio higher than  $2 \mu C/g$ .

$$
q_{\rm d}=\frac{4.75\pi\epsilon_0d_{\rm d}}{\ln(D_{\rm e}/d_{\rm j})}\eqno(87)
$$

$$
V_{\rm c} = f\lambda \tag{88}
$$

$$
V_{\rm c} = (4\sigma/\rho d_i)^{1/2} \tag{89}
$$

where  $\sigma$  is the surface tension,  $\rho$  is the density of the liquid, der coating rose in 1994, e.g., architectural finishing was up and  $d_i$  is the jet diameter.  $V_c$  is about 2 m/s. The excitation frequency *f* breaks the capillary into *f* drops per second. In a typical continuous ink jet operation, more than 100,000 drops, of approximately 100  $\mu$ m diameter, are produced per second.

# **POWDER COATING PROCESS**

## **Process Description**

Powder coating (3,15) is a multidisciplinary field comprising Charged powder powder technology and electrostatic engineering. It involves: **Figure 16.** A schematic showing a powder coating setup with a co tion and transport of powder, (4) particle charging and disper- kV is applied to the corona gun.

sion, (5) electrostatic spraying and coating, (6) curing and melt rheology, and (7) process modeling and optimization.

In an electrostatic coating process, the powder is first fluidized so that it can be pneumatically conveyed, at a controlled mass flow rate, from a reservoir to the spray gun, where it is electrostatically charged and sprayed toward the grounded workpiece to be painted (Fig. 16). The aerodynamic forces of the atomization air transport the charged particles from the spray gun to the vicinity of the workpiece. Near the surface of the workpiece, the electrostatic image force between the charged particles and the grounded metal surface dominates, causing the particles to deposit on the surface. Coating is performed in a powder coating booth. Workpieces to be coated are moved to the booth using a conveyor belt, and are then moved to an oven for curing the powder layer **Figure 15.** <sup>A</sup> continuous ink jet generator used for printing. (thereby forming a film) on the surface.

The four forces acting between the charged particles and the conducting substrate are: (1) the electrostatic image force For a droplet diameter not to exceed 100  $\mu$ m,  $d_j$  is chosen to of attraction between charged particles and the grounded be about 35  $\mu$ m; therefore,  $U_i$  is 15.75 m/s. A static pressure workniece (2) the coulombic rep arriving at the substrate and the deposited particles charged inter is shown in Fig. 15.<br>During the formation of the droplets, small satellite drop-<br>forces compete with each other, and the resultant forces bold the particles onto the workpiece until the coating is cured in

The droplet charge  $q_d$  can be written as **Electrostatic powder coating is an environmentally safe**, economically competitive, high-quality painting process for metals and plastics. The oversprayed powder can be recycled back into the coating process to achieve better than  $95\%$  material utilization. This high-efficiency application contrasts dramatiwhere  $d_d$  is the droplet diameter,  $D_e$  is the diameter of the<br>cylindrical electrode used for applying electric field, and  $d_j$  is<br>compounds (VOCs) used in most solvent-based coating pro-<br>the diameter of the ink jet.<br>A p *reused, resulting in considerable material loss.* 

The powder coating process has a large industrial base in where the United States, with a growth rate of  $10\%$ /yr or more, depending upon the specific industry. For example, as early as 1994, American powder coating sales were up by 15% over the same sales period in 1993. All market categories in pow-



(1) polymer science, (2) powder manufacturing, (3) fluidiza- rona gun and a flat grounded metal plate. A high voltage up to  $-100$ 

market opportunities. Automotive clear coats in particular to what was anticipated. Currently, manufacturers of powder may drive US industrial growth rates in powder coating up coating guns use a feedback control system to maintain a conto 10% or more annually through this decade. The big three stant corona current by varying the high voltage applied to US auto manufacturers—GM, Ford, and Chrysler—have the gun so as to minimize back corona. Back corona can be formed a low-emission paint consortium to advance powder observed under dark conditions as a diffuse glow on the powcoating. Other automotive companies, including BMW, have der surface. An image intensifier tube can be used to map begun adding top clear-coat using a powder spray process. back corona on a powder layer.

The greatest challenge faced by the powder coating industry<br>is to produce a surface finish comparable to, or even better<br>than, the solvent-based process. Current powder coating tech-<br>than, the solvent-based process. Curre of a dry process—environmental safety, high transfer efficiency, and cost-effectiveness in the painting of the exterior surface of the automobiles—will not be realized unless better appearance of the surface finish, chip resistance, and weath-<br>ering characteristics are achieved. For these purposes it will<br>be necessary to optimize the electrostatic properties, melt rhe-<br>ology, and surface chemistry of of powders on the target surface need to be controlled to minimize the orange-peel texture and to produce a glossy finish that will withstand outdoor exposure in Florida (Florida Exposure Test) for 20 years or more. The interstitial air in the porous powder layer will break

thermal properties may eventually make the process superior to solvent-based coating in all respects. Currently, both tribocharging and corona charging methods are used in the electrostatic spray painting process. However, corona charging is most widely used in the powder coating industry. The corona If the density of the powder layer is approximately 1000 discharge process is discussed in the section "Charging of Ma-  $\text{kg/m}^3$ , terials and Transport of Charged Particles'' above. The corona discharge results in a reproducible charging of powder; however, only a portion of the ion current is utilized in charging. Since the discharge produces large amounts of ions, the charged particles and the remaining ions deposit on the sub-<br>strates along with the powder layer. This ionic current powder layer of 100 um thickness when the charge-to-mass strates along with the powder layer. This ionic current powder layer of 100  $\mu$ m thickness when the charge-to-mass charges the powder layer and causes dielectric breakdown in ratio of the powder exceeds 1.77  $\mu$ C/g. In charges the powder layer and causes dielectric breakdown in ratio of the powder exceeds 1.77  $\mu$ C/g. In most applications, it, resulting in back corona. Back corona produces an orange-<br>charge-to-mass ratio varies from 0. it, resulting in back corona. Back corona produces an orange-<br>peel textured surface, unacceptable in many applications. breakdown electric field can be lower than 10<sup>7</sup> V/m. A mini-Surface textures can be controlled in the corona discharge method if the electrical resistivity can be optimized by appropriate powder formulation or by spraying powder at a high relative humidity, around 60%. Currently no method is readily applicable to control the volume resistivity of powders for powder coating applications.

When the gun voltage is increased or the gun-to-workpiece distance *d* is decreased, there is an increase of ion current [see Eq. 52(b)], which may increase back corona and reduce particle deposition efficiency even further. When the back co-

57%; lawn and garden, 26%; appliances, 17%; automotive, rona process was not well understood, powder coating process 20%; and general metal finishing, 9%. operators often would increase the gun voltage to improve Technological advances in powder coating may open large transfer efficiency, only to find that the outcome was opposite

Equation 52(a) shows how the ion current *I* increases with **Film Appearance** the voltage *V* applied to the gun. Since the charge-to-mass

$$
EA = \frac{q_{\rm v}At}{\epsilon_0 \epsilon_{\rm r}}\tag{90}
$$

$$
E_{\rm b} = \frac{q_{\rm v}t}{\epsilon_0 \epsilon_{\rm r}}\tag{91}
$$

down at  $E_b \approx 3 \times 10^6$  V/m.  $E_b$  will be much higher for a solid **Process Optimization and Reduction of Back Corona** film (see Table 5). If we consider the breakdown voltage of the Optimization of material formulation and electrostatic and powder layer is as high as  $10^7$  V/m, then maximum charge thermal properties may eventually make the process superior per unit volume, for  $t = 100 \mu m$  and  $\epsilon = 2$ 

$$
q_{\rm v} = 1.17 \,\mathrm{C/m}^3 \tag{92}
$$

$$
(q/m)_{\text{max}} = \begin{cases} 1.17 \,\mu\text{C/g} & \text{for} \quad E_{\text{b}} = 10^7 \,\text{V/m} \text{ (dielectric)} \\ 0.39 \,\mu\text{C/g} & \text{for} \quad E_{\text{b}} = 3 \times 10^6 \,\text{V/m} \text{ (air)} \end{cases} \tag{93}
$$

breakdown electric field can be lower than  $10^7$  V/m. A mini-

**Table 5. Dielectric Breakdown Field for Different Media**

Dielectric Medium	Breakdown Electric Field (V/m)
Air	$3\times10^6$
Polystyrene	$2.4 \times 10^{7}$
Teflon	$1 \times 10^7$
Barium titanate	$5 \times 10^6$
Mylar	$1.5 \times 10^{8}$

mum value of  $q/m$  of the powder is needed for good adhesion. One experimental study indicates that *q*/*m* should be larger than 0.2  $\mu$ C/g (3).

Tribocharging produces no ion current, but presently it is not reliable for consistent charging of the powder. Both fundamental and experimental research studies are needed to overcome some of the engineering problems. Current understanding of contact and tribocharging of nonconducting particles needs to progress to a level where electrostatic charging processes can be controlled in a quantitative manner. While the major engineering problems have been solved for toner charging in the electrophotographic process through extensive experimental studies, tribocharging is still considered unreliable and unpredictable for powder coating applications. For example, a typical powder coating system requires simultaneous operation of 16 powder coating guns, each delivering 60 g to 100 g of powder per minute. Once the inner walls of triboguns are coated with powder, the charging efficiency decreases. The triboguns to be used in the powder coating process must be able to operate continuously in a reliable manner.

# **ELECTROPHOTOGRAPHY: COPYING MACHINES AND LASER PRINTERS**

About the same time electrostatic precipitators became widely used in industry for removing particulate materials from gas, a new application of electrostatics was emerging electrophotography. Electrophotography is used in office copiers and laser printers, by far the most successful industrial ers and laser printers, by far the most successiul maustrial (c)<br>application of all electrostatic engineering processes. It accounts for approximately \$50 billion in annual sales in the **Figure 17.** (a) A corona-charged photoconducting drum. (b) A latent trostatic copying process, which merged two branches of phys-<br>ics, electrostatics and photoconductivity. For more details on letter "A" formed by the copying process. electrophotography, see ELECTROPHOTOGRAPHY.

Electrophotography (6,15,16) is similar to optical photogra-<br>phy, where a silver halide film is used to first store a latent<br>optical image on its surface. The film is then developed to<br>print the image on photographic paper  $\begin{tabular}{p{0.8cm}p{0.1cm}p{0.$ and thus toners need to be deposited on the discharged area. 3. *Development of the Latent Image*. Electrostatically<br>This is known as discharged area development (DAD) In the charged pigmented toner particles, with a size This is known as discharged area development (DAD). In the charged pigmented toner particles, with a size distribu-<br>conving process information is usually stored in black on a tion from 6  $\mu$ m to 8  $\mu$ m in diameter, dev copying process, information is usually stored in black on a tion from  $6 \mu m$  to  $8 \mu m$  in diameter, develop white hackground like this printed nage. An optical image white background, like this printed page. An optical image of a document on the photoconducting surface will therefore 4. *Transfer of the Developed Image.* The image developed discharge the background area (white), leaving the charged by the deposition of toner is then transferred from the area (black) with the information. In this case, a charged area photoconducting surface to an appropriate medium, development (CAD) is used, where toners are deposited on the such as paper or transparency, for use. A corona device



global economy. In 1937, Chester Carlson invented this elec- image of the letter "A" formed by a laser beam scanner on a positively<br>trostatic conving process, which merged two branches of phys. charged photoconducting film

- 
- 
- 
- charged surfaces. These processes are illustrated in Fig. 17. is used to spray charged ions on the back of the page to



- 
- *for the Next Cycle.* The cleaning process requires an ac corona discharge, so that charged particles still adher- **ELECTROSTATIC SEPARATION** ing to the photoconducting drum can be discharged and then dislodged by a mechanical cleaning brush. Simi- **Basic Mechanisms** larly, after fusing of the toner on the surface of the me-

machines, laser printers, and ink jet printers. These printing characteristics. In the first process, a rotating-drum separator<br>is generally used. Particles are fed from a vibrating hopper to<br>the processes are often collec

tain the desired surface finish after fusing of the toners on the medium's surface. Toners are always charged triboelec- **Electrostatic Beneficiation Process for Coal Cleaning** trically in one of two ways: (1) a two-component development process where toner particles are charged against carrier par- With the electrostatic cleaning method (14), coal is first pulticles (magnetic particles, coated with an appropriate polymer verized into a fine powder of particles 5  $\mu$ m to 750  $\mu$ m in layer, in the size range 50  $\mu$ m to 200  $\mu$ m in diameter) to pro- diameter. The powder is then electrostatically charged by imvide electrostatic charge of controlled magnitude and desired pact against a metal surface such as copper. On contact with

polarity to the toners; or (2) a one-component development process where toner particles are blended with magnetic materials that are triboelectrically charged against the surface of the development roller, and then against a doctor blade. The flow of toner particles from the reserve to the photoconducting drum is produced by the movement of the roller film over a bank of stationary magnets, which attract the magnetic toner to the surface of the roller. No carrier powder is used in this case.

In the two-component development process, the toner particles are attracted to the latent image on the photoconducting surface by the electrostatic attractive forces while the carrier particles are held on the development roller by magnetic forces. In the one-component development process, toner particles are made magnetic in order to facilitate the flow of toner by the development roller to the photoconducting drum.

Extensive theoretical and experimental studies have been Figure 18. An electrophotographic process showing six steps to<br>performed on the toner charging and development processes.<br>printing or copying: (1) charging, (2) latent-image formation, (3) im-<br>age development by charged t ficult to accurately analyze the process of toner development attract toners of opposite charge from the photoconducured because of the complexity of the electric field distributions<br>to to the paper.<br>5. Fusing of the Toner Particles on the Medium. The toners<br>5. Fusing of the Toner Pa

dium, the high electrostatic charge on the media must<br>alien, the high electrostatic charge on the media must<br>also be remeved to eliminate electrostatic cling and<br>feldspar, phosphate rock from silica sand, rubber from fabri also be removed to eliminate electrostatic cling and teldspar, phosphate rock from silica sand, rubber from fabric,<br>sparking.<br>diamond from gangue has been successfully demonstrated in Corona and tribocharging processes are involved in electro-<br>  $\frac{1}{2}$  laboratory experiments, pilot plant studies, and, in some<br>
cases, commercial plants  $(3,14,17-19)$ . The process is very atphotography, and exact control of the charging process is es-<br>sential for ensuring excellent performance of copying ma-<br>sential for ensuring excellent performance of copying ma-<br>chines and laser printers. It took more than processes are often collectively called nonimpact printing. is generally used. Particles are fed from a vibrating hopper to the surface of a conducting drum, which rotates at an opti-**Toner Charging and Development** mum rate. First the particles are charged in a corona charg-<br>ing zone. As the particles move further from the charging Toners are polymer particles 2  $\mu$ m to 20  $\mu$ m in diameter. The ing zone. As the particles move further from the charging polymers are polystyrenes, polyacrylics, polymethacrylites, or applying and fall off the drum. Th



the copper, the organic coal particles become positively gamic coal particles charged positively gamins copper. Kwet-<br>charged and the pyritse and inorganic innergal articles be-<br>nome negatively charged. If this tribocharg

many countries, as shown in Table 6. However, the process **Effect of Particle Concentration** has not been implemented on a commercial scale. Many fundamental aspects of the tribocharging process involved in In a commercial-scale operation, the particle concentration insemiconducting and insulating materials are not well under- side the separator will be high. Increasing particle concentra-

stood (6). Many factors influencing the efficiency of beneficiation also remain poorly understood. This is due in large part to the great complexity of coals, which have been subjected to biomorphic and geomorphic changes over very long time periods. Coal is a heterogeneous rock consisting of discrete maceral and mineral components, something like a fruitcake (19). Coals from diverse localities have widely differing compositions and structures and hence variable charging properties.

# **Electrostatic Charging of Coal and Minerals**

Coal particles under dry conditions and low relative humidity are insulators with resistivity approximately  $10^{14} \Omega \cdot m$ , whereas pyrite particles are semiconductors with a resistivity of  $10^7$   $\Omega$  m. The resistivity of coal particles will depend greatly upon their moisture and ash content, and thus different types of coal will have different resistivity. For insulators that are partly amorphous, the lattice structure is disordered and there are localized energy levels within the bandgap, due both to the discontinuities in the normal structure of the material at the surface and to the presence of impurity atoms. The surface of coal has abundant impurities. Discontinuities and the impurity atoms at the surface contribute to the intrinsic and extrinsic surface states. Figure 12 shows the contact charging process between coal and copper.

Inculet et al. (20) observed that vitrinite macerals have a tendency to be positively charged, while fusinite and semifusinite charge negatively. Experimental data obtained by them in coal fractions separated in an electrostatic process indicate that while a major fraction of the vitrinite charged positively, a significant portion charged negatively. Most of the pyrites, however, charged negatively. More recently Kwetkus (21) studied coal samples from France, Great Britain, and the **Figure 19.** Electrostatic physical cleaning of coal. United States and found that in most cases the coal particles charged negatively. However, when run-of-mine (ROM) coal was processed by flotation to reduce the ash content, the or-

Year	Country	Description
1914	<b>United States</b>	Schniewend—patent on triboelectric separation of coal
1940	Germany	Pilot plant studies—reduction of ash $(15\% \text{ to } 1.5\%)$
1976	<b>United States</b>	Singewald—pilot plant operation with 5 ton/h feed rate
1977	Canada	Inculet—electrostatic loop separator
1983	Japan	Masuda—cyclone triboelectric separator
1984	Italy	Ciccu—rotating-wheel impact tribocharger
1987	<b>United States</b>	Gidaspow and Wasan—Electrofluidized bed and electrostatic sieve conveyors
1987	<b>United States</b>	Advanced energy dynamics (AED)—drum-type separator
1990	<b>United States</b>	Link and Finseth (DOE/PETC)—static copper charger and separator dynamics
1992	China	Chen—drum separator
1995	United States	Stencel (AER, KY)—workshop on dry separation technology

**Table 6. Milestones in Electrostatic Separation of Coal from Minerals**

tion has two attendant problems: (1) there will be a signifi- mable in a limited range of particle concentration (usually 80 cant space charge between the two electrodes, which will  $g/m^3$  to 2000  $g/m^3$  depending upon the particle size distribuinterfere with the separation, and (2) the frequency of inter- tion and the composition of the powder. As the effective partiparticle collisions will be high, causing coagulation of positive cle size decreases, specific surface area increases and combusand negative particles and thus decreasing the separation ef- tible dust becomes more ignitable. Similarly, there is a ficiency. It is anticipated that most of the collisions will be minimum oxygen concentration requirement for ignition. related to the turbulent shear stress, which increases with Also, the energy of the ignition source must be equal to or the flow Reynolds number. The number of particle collisions greater than the minimum ignition energy (MIE) for exper second can be estimated as  $(14)$  plosion.

$$
n = 0.27C \frac{du}{dy} \frac{d_{\rm p}^{1/2}}{\lambda^{1/2}} \tag{94}
$$

the particle stream,  $\lambda$  is the mean free path of the particles ship. (the average distance between collisions), and *du*/*dy* is the velocity gradient in a turbulent air flow. Since the number of collisions will increase with residence time, it will be necessary to reduce the residence time and therefore increase the The probability of explosion,  $P_e$ , can be expressed as velocity. However, since turbulence will increase the collision frequency, the separator must be designed to have minimum flow fluctuations.

Inherent in any physical cleaning process is the assumption presence of an ignition source with MIE. that the materials to be separated can be physically liberated For example, during the filling of a tank with combustible from each other. For the electrostatic beneficiation of coal, the powder or a liquid, charge can accumulate until a condition mineral particles must be liberated from the coal matrix dur- is reached when the stored electro mineral particles must be liberated from the coal matrix during crushing and grinding. Liberation of pyrites has been released by a spark exceeding the MIE, causing explosion. studied by Irdi et al. (22) and by Dumm and Hogg (23) using Triboelectric charge generation in the pneumatic transport froth flotation and density separation, respectively. The effect of powder can be as high as 100  $\mu$ C/kg. A large volume of of particle size distribution on the efficiency of beneficiation stored powder with such high specific charge per unit mass has been studied in some cases. **presents** ignition hazards. When the resistivity of the powder

oxygen gas, and (3) an ignition source such as an electrostatic discharge or a lighted match. Many airborne dusts are flam-

The MIE required to ignite powder at a given concentra $t_n = 0.27C \frac{du}{dy} \frac{d_p^{1/2}}{\lambda^{1/2}}$  (94) tion increases with the mean particle diameter  $d_{50} (\mu m)$ . For example, for polyethylene and aluminum flakes, the MIE varies from 10 mJ to 500 mJ as  $d_{50}$  increases from 0.1  $\mu$ m to where *C* is the concentration of particles, *u* is the velocity of 10,000  $\mu$ m according to the approximate empirical relation-

$$
MIE = \phi(d^3)
$$
 (95)

$$
P_{\rm e} = P_{\rm f} P_{\rm i} \tag{96}
$$

**Particle Size Effect P** is the probability of existence of a flammable pow-<br>der–air mixture and  $P_i$  is the probability of the simultaneous

is higher than  $10^{12} \Omega \cdot m$ , the charge relaxation time constant ELECTROSTATIC HAZARD CONTROL: ELECTROSTATIC is sufficiently long to pose ignition hazards due to accumula-<br>DISCHARGE BY DUST EXPLOSION When it is greater than 60% the charge decays quickly and

Electrostatic discharge (ESD) (4) may cause explosion in an the risk of ignition decreases significantly.<br>
atmosphere where a combustible powder or vapor is dispersed<br>
in air. Since many polymeric powders are highly resis

$$
U_{\rm e} = \frac{1}{2}CV^2 \ge \text{MIE} \tag{97}
$$

$$
V_{\text{max}} \le 350\,\text{V} \tag{98}
$$

In general, an upper limit of 100 V is used to supply a margin cause brush discharge.<br>
of safety. As a rule of thumb, when  $V$  exceeds 100 V, there is Preumatic transport of safety. As a rule of thumb, when *V* exceeds 100 V, there is Pneumatic transport of flammable powder can also be haz-<br>a chance of electrostatic spark.

not a cause of electrostatic ignition. Spark discharge is much by using metal tubes of large diameter to reduce friction dur-<br>more energetic than corona discharge. Sparking represents a ing filling. The danger is small whe more energetic than corona discharge. Sparking represents a ing filling. The danger is small when the powder transported negative resistance condition causing a high flow of current is not stored. For example, in a powder negative resistance condition causing a high flow of current is not stored. For example, in a powder coating process, insu-<br>for a very short duration.

The propagating brush discharge is perhaps one of the is deposited on a metal surface and is not stored in a large<br>most common sources of ESD ignition. When an insulating volume the ESD hazard is minimal. However, the meta most common sources of ESD ignition. When an insulating volume, the ESD hazard is minimal. However, the metal<br>layer on a conductive backing accumulates a high surface workniece receiving the charged powder must be well layer on a conductive backing accumulates a high surface workpiece receiving the charged powder must be well<br>charge density and comes close to a conducting object, it is grounded to minimize ESD ignition bazards. For resin charge density and comes close to a conducting object, it is grounded to minimize ESD ignition hazards. For resin pow-<br>possible to have an ESD with spark energy much greater dentified MIE is approximately 5 mJ; therefore t possible to have an ESD with spark energy much greater der, the MIE is approximately 5 mJ: therefore, the spark en-<br>than the MIE. A typical brush discharge condition is shown ergy needs to be maintained below 0.5 mJ for po in Fig. 20. The maximum surface charge that can accumulate der coating applications. on the insulating layer can be much higher than the maximum surface charge density for an isolated body. The insulat-<br>ing layer on a conductive backing acts like a distributed ca-<br>**Static Charges on a Human Body** pacitor by storing energy. When the charged insulating Electrostatic charge on a human body can also cause ignition<br>layer comes close to a conducting object, an electrostatic hazard. People walking on an insulating floor w charge may run along the surface. Therefore, it is not recom- lated shoes and nylon clothing, or touching electrostatically<br>mended to use plastic lining against a metal pipe for trans-<br>charged objects, can acquire a potent mended to use plastic lining against a metal pipe for trans-<br>port of powder. The capacitive energy per unit area can be capacitance of a human body is 200 pF. When a person with written as **a** high charge touches a grounded conductor, the spark energy

$$
U_{\rm e} = \frac{1}{2} C_{\rm L} V_{\rm L}^2 \tag{99}
$$
 cases.

 $V_{\rm L} = \sigma_{\rm s}/C_{\rm L}$  J spasm or even death may occur.  $\sigma_{s}$  = surface charge per unit area

Ignition is possible when  $U_e$  becomes greater than 1.2 **ESD Hazard Control**  $mJ/cm<sup>2</sup>$  in a brush discharge. When the surface charge is The following safety procedures are generally recommended. greater than 25 nC/cm2 , the thickness *t* of the insulating layer should be much larger than 1 mm. A propagating brush dis-<br>
charge can have energy release in excess of 1 J.<br>
In silos, most dust explosions are caused by *Maurer dis-*<br>
charge during the filling. Particles of diameter lar

*charge* during the filling. Particles of diameter larger than a



**Figure 20.** An insulating film or powder layer accumulating charge can be discharged to a grounded object with propagating brush dis-<br>charge, causing ignition. When the surface charge density exceeds<br> $3 \times 10^{-6} \mu C/m^2$ , t  $3 \times 10^{-6} \mu$ C/m<sup>2</sup>, there is a probability of brush discharge (1–3 mJ). A propagating brush discharge (100 J) occurs when the surface charge density exceeds  $2 \times 10^{-4}$  C/m<sup>2</sup> on a thin insulating layer over a grounded conducting surface.

The maximum sparking potential voltage  $V_{\text{max}}$  must satisfy few hundred micrometers do not cause ESD ignition hazard, but fines, which are almost always present, can result in a flammable atmosphere. During the filling operation, larger particles acquire charge because of their higher velocity and

chance of electrostatic spark.<br>It is important to note that corona discharge is, in general, locity of the powder it is possible to avoid ESD ignition risk It is important to note that corona discharge is, in general, locity of the powder, it is possible to avoid ESD ignition risk<br>not a cause of electrostatic ignition. Spark discharge is much by using metal tubes of large dia a very short duration.<br>The propagating brush discharge is perhaps one of the is deposited on a metal surface and is not stored in a large ergy needs to be maintained below 0.5 mJ for powders in pow-

hazard. People walking on an insulating floor wearing insucapacitance of a human body is 200 pF. When a person with can be as high as 10 mJ, which can exceed the MIE in some

The human reaction to ESD depends upon the energy of where the spark. Below 1 mJ, the ESD is often not detectable. At 10 mJ, there is a pricking sensation; at 100 mJ, the electric  $C_{\text{L}}$  = capacitance per unit area =  $\epsilon_{\text{r}}\epsilon_{0}/t$  shock is unpleasant; above 1 J it is painful; and at about 100

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	- b. Increase the relative humidity.
	- c. Use antistatic materials.
	- d. Use thin rods or static bars (1 mm to 3 mm diameter) inside the storage silos. Ground the rods well to promote corona discharge or brush discharge in discharging the powder store.
	- e. Neutralize charges by using a pointed metal rod connected to the ground and placed inside a pipe with the tip projecting into the powder flow stream, which may initiate corona discharge and generate ions for neutralization.
- increases the surface conductivity of many polymer ma-

the recommended safe upper limit of potential difference is Effect of surface ox<br>100 V Most sensitive devices should be grounded with resis. 1989, pp. 327–330. 100 V. Most sensitive devices should be grounded with resis-<br>tance no greater than 10<sup>6</sup> O. A grounding resistance also de. 8. J. Lowell and A. C. Rose-Innes. Contact electrification. Adv. tance no greater than  $10^6 \Omega$ . A grounding resistance also de-<br>*Phys.*, **29**: 947–1023, 1980.<br>*Phys.* **29:** 947–1023, 1980. creases the energy of the spark.

Active Charge Neutralizers. Bipolar ionizers can be used to<br>neutralize static electricity. In this case, the charge is not discussed to<br>neutralize static electricity. In this case, the charge is not discussed to<br>general t

Neutralization Using a Radioactive Source. In some cases Studies Press and Wiley, 1985. where conventional ionization process cannot be used, partic-<br>
16. E. M. Williams, *The Physics and Technology of Xerographic Pro*ularly in areas where electrical devices may create additional *cesses,* New York: Wiley, 1984. hazards, radioactive sources are used for air ionization. Polo- 17. O. C. Ralston, *Electrostatic Separation of Mixed Granular Solids,* nium-210, an alpha source, is commonly used to produce Amsterdam: Elsevier, 1961. strong ionization in a small confined area. Krypton-85, a beta 18. D. Whitlock, Advanced physical fine coal cleaning, Advanced Enemitter, is also used to neutralize charged particles at a low ergy Dynamics Report, DOE Contract #DE-AC22-85PC81211, concentration. December 1987.

**Induction Ionizers.** Induction ionizers are commonly used beneficiation of coal, *Inst. Phys. Conf. Ser. 143,* 1996, p. 385. **Inst. Phys. Poneficiation** of coal, *Inst. Phys. Conf. Ser. 143,* 1996, p. 385. **Instemate in t** to neutralize areas of high static charge generation. Typically, 20. I. I. Inculet, M. A. Bergougnou, and J. D. Brown, Electrostatic<br>these passive neutralizers consist of sharp, grounded beneficiation of coal, in Y. A. Liu needlepoints placed opposite charged surface. The induced<br>charge  $\frac{Coal—Present and Developing Methods$ , New York: Marcel Dek-<br>charge at the needlepoint causes corona discharge, thereby<br>reducing ions to neutralize charges. For neutralization the 2 producing ions to neutralize charges. For neutralization, the <sup>21. B.</sup> A. Kwetkus, Contact electrication of coal and minerals, *J.* charge induced must be high enough to initiate corona dis-<br>charge. 22. G. A. Irdi, S. W. M

Static Bars. Static bars are arrays of bars used to inject ions<br>either by corona discharge or by using nuclear radiation. Such<br>static change generalism and R. Hogg, Distribution of sulfur and ash in ul-<br>static bars are oft ation. ence, 1987.

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